

(b) Using the method of Lagrange's multiplier solve the N.L.P.

$$\text{Optimise } z = 12x_1 + 8x_2 + 6x_3 - x_1^2 - x_2^2 - x_3^2 - 23.$$

$$\text{Subject to } x_1 + x_2 + x_3 = 10. \quad x_1, x_2, x_3 \geq 0. \quad [6]$$

(c) Marks obtained by students in an examination follow normal distribution. If 30 %

Of the students got below 35 marks and 10 % got above 60 marks. Find the mean and standard deviation. [8]

Q4 (a) Find the Eigen values and Eigen vectors of matrix $A = \begin{bmatrix} 3 & 10 & 5 \\ -2 & -3 & -4 \\ 3 & 5 & 7 \end{bmatrix}$ [6]

(b) Find inverse z- transform of $F(z) = \frac{3z^2 - 18z + 26}{(z-2)(z-3)(z-4)}$ $3 < |z| < 4$. [6]

(c) Using the Kuhn –Tucker conditions solve the N.L.P [8]

$$\text{Maximise } z = 12x_1x_2 + 2x_1^2 - 7x_2^2$$

$$\text{Subject to } 2x_1 + 5x_2 \leq 98;$$

$$x_1, x_2 \geq 0.$$

Q5 (a) Show that the matrix $A = \begin{bmatrix} -9 & 4 & 4 \\ -8 & 3 & 4 \\ -16 & 8 & 7 \end{bmatrix}$ is diagonalisable. Find the diagonal

form D and the Diagonalising matrix M. [6]

(b) Find the relative maximum or minimum of the function

$$z = x_1^2 + x_2^2 + x_3^2 - 4x_1 - 8x_2 - 12x_3 + 100. \quad [6]$$

(c) Evaluate $\oint \frac{2z-1}{(2z+1)z(z+2)} dz$ using Cauchy's residue theorem, where C is the circle $|z| = 1$. [8]

Q6 (a) The number of car accidents in a metropolitan city was found to be 20, 17, 12, 6, 7, 15, 8, 5, 16 and 14 per month respectively. Use χ^2 - test To check whether these frequencies are in agreement with that occurrence was The same during 10 months period. Test at 5 % level of significance. [6]

(b) Find z – transform of $[2^k \cos (3k + 2)] , k \geq 0 .$ [6]

(c) Use the dual simplex method to solve the L.P.P. [8]

Minimise $z = 2x_1 + x_2$
 Subject to $3x_1 + x_2 \geq 3;$
 $4x_1 + 3x_2 \geq 6;$
 $x_1 + 2x_2 \leq 3;$
 $x_1, x_2 \geq 0.$
