

Time: 3 Hours**Marks 80****N.B. : (1) Question No 1 is Compulsory.****(2) Attempt any three questions out of the remaining five.****(3) All questions carry equal marks.****(4) Assume Suitable data, if required and state it clearly.**

- 1 Attempt any FOUR [20]
- a Calculate the average power of $20\cos 100t$ 5
- b Describe RLC circuit by differential equation 5
- c Explain the conditions for the existence of Fourier transform 5
- d Determine the relationship between CTFT and LT 5
- e Find the z-transform of $x(n) = a^n u(n)$ and sketch the RoC 5
- 2 a $x(t) = 2, 0 \leq t \leq 5$ [10]
 $= 0, \text{ elsewhere}$
Sketch $x(t), x(-t), -x(t), x(t-2), x(t+3), 2x(t), x(2t), x(t/2), x(t) + x(-t)$ and $x(t) - x(t-2)$
- b Find $x[n]$ using partial fraction method from $X(z) = \frac{3 + 2z^{-1} + z^{-2}}{1 - 3z^{-1} + 2z^{-2}}$ [10]
- 3 a For a LTI system, input $x(t)$ and impulse response $h(t)$ are given below. Find the output using convolution. [10]
 $x(t) = h(t) = A, -T \leq t \leq T$
 $= 0, \text{ elsewhere}$
- b Realize the given IIR system using canonic structure. [10]
 $y[n] = -3y[n-1] + 3y[n-2] + y[n-3] + x[n] + 3x[n-1] + 2x[n-2]$
- 4 a State and prove sampling theorem for low pass signal using Fourier transform [10]
- b Find the autocorrelation function and average power of a periodic signal $A \cos \omega_0 t$ [10]
- 5 a Find the Laplace transform of $x(t) = e^{at}$ where $a > 0$ and sketch the RoC. [10]
- b Find the transfer function $H(z)$ and impulse response $h[n]$ of a discrete time system with I/O relation $y[n] - 0.5y[n-1] = x[n] + 2x[n-1]$ [10]

- 6 a $x[n] = [2, -1, 3, \underline{1}]$. Sketch $x[n]$, $x[n+2]$, $x[n-2]$, $x[-n]$, $x[-n+2]$, $x[-n-2]$, $x[2n]$, $x[n/2]$, $-x[-n]$ and $x[n-2] + x[n+1]$. Underline in $x[n]$ shows the 0th position. [10]
- b State and prove modulation theorem using Fourier transform [10]