SE-ECS / Sem-IV / R-19 / FH-25 / Dt: 13-05-20

Op: 83229

25

(3 Hours) [Total Marks: 80]

N.B.: 1) Question No. 1 is **Compulsory.**

2) Answer **any THREE** questions from Q.2 to Q.6.

3) Figures to the right indicate full marks.

Q.1 (a) Find (i) k (ii) mean and variance of the following distribution (5)

X	8	12	16	20	24
P(X)	1/12	5/12	k	1/4	1/12

(b) Evaluate $\int_c (x - iy^2)dz$ where c is curve $x = y^2$ from point (0,0) to (1,1). (5)

(c) Find the extremal of $\int_0^{3\pi/2}(y^2 - y'^2)dx$ where y(0)=0 ; y(3π/2)=1 (5)

(d) State and verify the Cauchy Schwarz for the vectors (2, 1, 1,-1) and (1,-2, 1, 1). (5)

Q.2 (a) Evaluate $\int_c \frac{z}{(z^2+3z+2)}dz$, where c is the circle $|z + 1| = 1/2$. (6)

(b) Fit the second degree polynomial for following data (6)

Price(X)	20	16	10	11	16
Demand(Y)	22	41	120	89	56

(c) Transform the basis {(1,0,1) ; (1,1,0);(0,1,1)} into orthogonal basis using Gram-Schmidt process. (8)

Q.3 (a) Check whether the following sets are subspace of R^3 (6)

(i) W={(a ,0,0)/ a belongs toR }

(ii) W={(x ,y, z)/$x^2+y^2+z^2 \leq 1$}

(b) Calculate the rank correlation coefficient 'R' for the following data (6)

x	10	12	18	16	15	40
y	12	18	20	15	50	25

(c) Obtain all possible Laurent's series expansion of $f(z) = \frac{1}{z^2+12z+35}$ about $z = 0$. (8)

Q.4 (a) If X and Y are independent random variable with $E(X) = 6$ and $E(Y) = -6, V(X) = 4, V(Y) = 9$ then find (6)

i) $E(2X + 3Y - 2)$

ii) $V(3X + 2Y + 2)$

(b) Evaluate $\int_0^{1+i} (x - y + ix^2)\, dz$ along the line from $z = 0$ to $z = 1 + i$. (6)

(c) Find rank, index, signature and nature of the Quadratic form by reducing it into Canonical form by congruent transformation $x^2 + 3y2 + 3z^2 - 2yz$. (8)

Q.5 (a) Three factories A, B, C produce 30%, 50% and 20% of the total production of an item. Out of their production 80%, 50% and 10% are defective respectively. An item is chosen at random and found to be defective. Find the probability that it was produced by the factory A. (6)

(b) A continuous random variable has pdf $f(x) = k(x - x^2), 0 \le x \le 1$. Determine k, mean, and variance. (6)

(c) Using Rayliegh -Ritz method solve boundary value problem (8)

$\int_0^1 (2x^2 y - 4y^2 + y'^2)dx$, y(0)=0 , y(1)=0.

Q.6 (a)

x	65	66	67	67	68	69	70	72
y	67	68	65	68	72	72	69	71

(6)

Calculate the Karl Pearson's coefficient of correlation.

(b) Find the extremals of $\int_a^b (16y^2 - y''^2 + x^2)dx$. (6)

(c) Given: $6y = 5x + 90$, $15x = 8y + 130$ are regression lines and $\sigma_x^2 = 16$ then find (i) mean of X and Y (ii)correlation coefficient (r) $(iii)\sigma_y^2$. (8)