Paper / Subject Code: 51021 / Engineering Mathematics - III

02:30 pm - 05:30 pm 1T00833 - S.E.(Electrical Engineering)(SEM-III)(Choice Base Credit Grading June 4, 2024 System) (R- 19) (C Scheme) / 51021 - Engineering Mathematics - III QP CODE: 10057278

(3 Hours) Total Marks: 80

Note: 1) Question 1 is compulsory.

- 2) Attempt any 3 questions from Question 2 to Question 6
- 3) Figures to the right indicate full marks.

Q1 Attempt All questions

A If
$$A = \begin{bmatrix} -1 & 2 & 3 \\ 0 & 3 & 5 \\ 0 & 0 & -2 \end{bmatrix}$$
 then find the Eigen values of $A^3 + 5A + 8I$

- Find Laplace transform of $f(t) = te^{3t} \sin 4t$ В
- Find the half range Fourier sine Series for $f(x) = x^2 + 1$ \mathbf{C} where $x \in (-\pi, \pi)$
- Prove that $f(z) = x^2 y^2 + 2ixy$ is analytic and also find its derivative D

Using Green's theorem in a plane to evaluate the line integral

$$\oint_C (x^2 - y)dx + (2y^2 + x)dy$$

Around the boundary of the region defined by $y=x^2$ and y

- Find the Eigen values and Eigen vectors of the matrix $A = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$
 - Show that the function $y = 3x^2y + 6xy y^3$ is harmonic function and find the 8 corresponding analytic function.

- If $\bar{F} = x^2 z i 2y^3 z^3 j + xy^2 z^2 k$ find div \bar{F} and curl \bar{F}
- Find the orthogonal trajectories of the family of curves $3x^2y y^3 = c$ 6
- Verify Cayley-Hamilton theorem for the matrix A and hence find A-1 and A4 8

where
$$A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$

Using Stokes theorem to evaluate $\int_C \bar{F} \cdot d\bar{r}$ Where $\bar{F} = 4xzi - y^2j + yzk$ and C is the area in the plane z=0 bounded by 6

 $x=0, y=0 \text{ and } x^2 + y^2 = 1$

- Evaluate $\int_0^\infty \frac{e^{-t}\sin t}{t} dt$, using Laplace transforms 6
- Using Convolution theorem find $L^{-1}\left[\frac{s^2}{(s^2+1)(s^2+4)}\right]$ 8

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 $(3xz^2$

Q5

Find $L\{tcos^3t\}$ A

Consider the vector field \bar{F} on \mathbb{R}^3 defined by В $\bar{F}(x, y, z) = (6xy + z^3)i + (3x^2)$

- Show that \overline{F} is irrotational.
- Expand $f(x) = lx x^2$, $0 \le x \le l$ \mathbf{C} in a half-range (i)cosine series (ii) sine series

- **Q6**
- Obtain Fourier series expansion of f(x) = 4A in (-2, 2)

Prove that the matrix A is diagonalisable В

- \mathbf{C}