## Paper / Subject Code: 51401 / Applied Mathematics-III

## S.E. SEM - III / I.T. / CHOICE BASE / MAY 2019 / 08.05.2019

**Total Marks: 80** 

Hours: 3 hrs

Note: 1) Question no. 1 is compulsory.

2) Attempt any three questions out of five questions

Q-1

- a) If any 11 numbers between 1 and 20 are chosen show that at least two of them will be multiplies of each other. (05)
- b) A function  $f: R \left\{\frac{7}{3}\right\} \to R + \left\{\frac{4}{3}\right\}$  is defined by  $f(x) = \frac{4x 5}{3x 7}$ , Prove that f is bijective

and find the rule for  $f^{-1}$ .

c) Find 
$$L\left[\frac{d}{dt}\left(\frac{1-\cos 2t}{t}\right)\right]$$
 (05)

d) Prove that there does not exist an analytic function whose imaginary part is

$$3x^2 + \sin x + y^2 + 5y + 4$$
. (05)

0-2

a) Find 
$$L^{-1} \left[ \frac{s}{(s^2 + 3^2)(s^2 + 5^2)} \right]$$
 using convolution Theorem. (06)

b) What is the chance of throwing ten with four dice? (06)

c) In a certain examination there are multiple choice questions. There are four possible answers to each questions and one of them is correct. An intelligent student can solve 90% questions correctly by reasoning and for the remaining 10% questions he gives answer by guessing. A week student can solve 20% question correctly by reasoning and for the remaining 80% questions he gives answer by guessing. An intelligent student gets the correct answer. What is the probability that he was guessing. (08)

Q-3

a) A can hit a target 2 times in 5 shots, B 3 times in 4 shots, C 2 times in 3 shots. They fire a volley. What is the probability that at least 2 shots hit the target? (06)

b) Find 
$$L^{-1}\left(\tan^{-1}\left(\frac{2}{s^2}\right)\right)$$
 (06)

c) If R is the relation on the set of integers such that aRb if and only if 2a+3b is divisible by 5. Find the equivalence classes. (08)

0-4

a) Evaluate 
$$\int_{t=0}^{\infty} e^{-3t} \left( \frac{\cos(7t) - \cos(11t)}{t} \right) dt$$
 (06)

b) Find 
$$L^{-1} \left[ \frac{s^2 + 2s + 3}{(s^2 + 2s + 10)(s^2 + 2s + 17)} \right]$$
 (06)

c) Find the bilinear Transformation which maps the points 2, i, -2 on to the points 1, i, -1. Also find image of |z| = 1 of z-plane to w-plane. (08)

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0-5

a) A family consisting of an old man, 6 adults and 4 children is to be seated in a row for dinner. The children wish to occupy two seats at each end and the old man refuse to have a child on either side of him. In how many ways can the seating arrangement be made for the dinner?

(06)

b) Find the analytic function f(z) = u + iv in terms of z if  $u - v = (x - y)(x^2 + 4xy + y^2)$ .

(06)

c) Solve 
$$\frac{d^3y}{dt^3} - 2\frac{d^2y}{dt^2} + 5\frac{dy}{dt} = 0$$
 with  $y(0) = 0$ ,  $y''(0) = 0$ ,  $y'''(0) = 1$ . (08)

Q-6

- a) Prove that  $(A-B) \cup (B-A) = (A \cup B) (A \cap B)$  (06)
- b) Draw the Hasse diagram of  $D_{105}$ . (06)
- c) Find Laplace Transformation of the following

i) 
$$te^{3t}erf(5\sqrt{t})$$
,

ii) 
$$\sin t H(t) + (\cos t - \sin t) H(t - \pi)$$
 (08)

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