## Q.P. Code: 25227

Duration: 3hrs [Total Marks: 80]

- 1) Question no.1 is compulsory.
- 2) Solve any three questions out of remaining five questions.
- 3) All questions carry equal marks as indicated by figures to the right.
- 4) Assume appropriate data whenever required. State all assumptions clearly.



(05M)

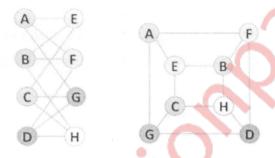
b) Find the generating function for the following finite sequences

(05M)

i) 2,2,2,2,2,2

ii) 1,1,1,1,1,1

- c) A box contains 6 white balls and 5 red balls. In how many ways 4 balls can be drawn from the box if, i) they are to be of any color ii) all the balls to be of the same color. (05M)
- d) Find the complement of each element in D<sub>30</sub>. (05M)
- Q.2 a) Define Isomorphism of graphs. Find if the following two graphs are isomorphic. If yes, find the one-to-one correspondence between the vertices. (08M)



- b) In a certain college 4% of the boys and 1% of the girls are taller than 1.8 mts. Furthermore 60% of the students are girls. If a student selected at random is taller than 1.8 mts, what is the probability that the student was a boy? Justify your answer (08M)
- c) Prove  $\neg (p \lor (\neg p \land q))$  and  $\neg p \land \neg q$  are logically equivalent by developing a series of logical equivalences.
- Q. 3 a) Prove that set  $G = \{1,2,3,4,5,6\}$  is a finite abelian group of order 6 with respect to multiplication module 7. (08M)
  - b) Let  $A=\{1,2,3,4,5\}$ , let  $R=\{(1,1),(1,2),(2,1),(2,2),(3,3),(3,4),(4,3),(4,4),(5,5)\}$  and  $S=\{(1,1),(2,2),(3,3),(4,4),(4,5),(5,4),(4,5)\}$  be the relations on A. Find the smallest equivalence relation containing the relation R and S. (08M)

c) Test whether the following function is one-to-one, onto or both.

(04M)

f:  $Z \rightarrow Z$ ,  $f(x)=x^2+x+1$ 

Q.4 a) Show that the (2,5) encoding function e: $B^2 \rightarrow B^5$  defined by

(08M)

e(00)=00000 e(01)=01110

e(10)=10101 e(11)=11011 is a group code.

How many errors will it detect and correct?

b) Let H=

Be a parity check matrix. Determine the group code  $e_H: B^3 \rightarrow B^6$ 

(M80)

- c) How many friends must you have to guarantee that at least five of them will have birthdays in the same month? (04M)
- Q.5 a) Let G be a set of rational numbers other than 1. Let \* be an operation on G defined by a\*b=a+b-ab for all a,b  $\in$ G. Prove that (G,\*) is a group.

b) Solve 
$$a_r-7a_{r-1}+10a_{r-2}=6+8r$$
 given  $a_0=1$ ,  $a_1=2$ 

(M80)

c) Let A={a,b,c,d,e,f,g,h}. Consider the following subsets of A

(04M)

 $A1=\{a,b,c,d\}$ 

 $A2=\{a,c,e,g,h\}$ 

 $A3={a,c,e,g}$ 

 $A4=\{b,d\}$ 

 $A5 = \{f,h\}$ 

Determine whether following is partition of A or not. Justify your answer.

i) {A1, A2} ii) {A3, A4, A5}

- Q.6 a) Draw the Hasse Diagram of the following sets under the partial order relation divides and indicate which are chains. Justify your answers. (08M)
  - I.  $A=\{2,4,12,24\}$
  - II.  $A=\{1,3,5,15,30\}$
  - b) Let the functions f,g, and h defined as follows:

(08M)

 $f:R \rightarrow R$ , f(x)=2x+3

g:  $R \rightarrow R$ , g(x)=3x+4

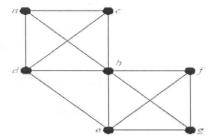
h: R $\rightarrow$ R, h(x)=4x

Find gof, fog, foh, , gofoh

Q.P. Code: 25227

c) Determine Euler Cycle and path in graph shown below

(04M)



Page 3 of 3

2FEE6430A725D77A0463A14A53E44801