

Duration: 3 Hrs

Total Marks: 80

Please check whether you have got the right question paper

- N.B:** (1) Question 1 is **compulsory**.
 (2) Attempt any **Three questions** out of remaining **Five questions**.
 (3) Assume any **necessary data**, if required, but **justify the same**.
 (4) **Figures** to the **right** indicate **full marks** for that question.
 (5) Use of Scientific **calculator** is **allowed**.

- Q.1 a) Solve the following LPP using Graphical Method [10]
 Maximize $Z = 20x_1 + 35x_2$
 Subject to $3x_1 + 3x_2 \leq 36$
 $5x_1 + 2x_2 \leq 50$
 $2x_1 + 6x_2 \leq 60$
 $x_1, x_2 \geq 0$
- b) A small project is composed of 7 activities whose time estimates are listed below. Activities are being identified by their beginning (i) and ending (j) node numbers. [10]

Activities		Times in week		
i	j	Optimistic time	Most likely time	Pessimistic time
1	2	1	1	7
1	3	1	4	7
1	4	2	2	8
2	5	1	1	1
3	5	2	5	14
4	6	2	5	8
5	6	3	6	15

1. Draw the network
2. Calculate the expected variances for each
3. Find the expected project completed time
4. Calculate the probability that the project will be completed at least 3 weeks than expected
5. If the project due date is 18 weeks, what is the probability of not meeting the due date?

- Q.2 a) Solve the following LPP using Simplex Method. [10]
 Maximize $Z = 2x_1 + 5x_2$
 Subject to $x_1 + 4x_2 \leq 24$
 $3x_1 + x_2 \leq 21$
 $x_1 + x_2 \leq 9$
 $x_1, x_2 \geq 0$

- b) The Captain of a cricket team has to allot the five middle batting positions to five Batsmen. The average runs scored by each batsman at these positions are as follows: [10]

Batsman	Batting Position				
	I	II	III	IV	V
P	40	40	35	25	50
Q	42	30	16	25	27
R	50	48	40	60	50
S	20	19	20	18	25
T	58	60	59	55	53

Find the assignment of batsman to positions which will give the maximum number of runs.

- Q.3 a) Solve the following using Big-M Method [10]

$$\begin{aligned} \text{Minimize } Z &= 2X_1 + 4X_2 \\ \text{Subject to } 2X_1 + X_2 &\leq 18 \\ 3X_1 + 2X_2 &\geq 30 \\ X_1 + 2X_2 &= 26 \\ \text{and } x_1, x_2 &\geq 0 \end{aligned}$$

- b) Find the initial basic feasible solution for the following transportation problem by Vogel's approximation method. [10]

	M1	M2	M3	Capacity
W1	26	23	10	61
W2	14	13	21	49
W3	16	17	29	90
Requirement	52	68	80	

- Q.4 a) Two firms are competing for business under conditions so that one firm's gain is another firm's loss. Firm A's pay-off matrix is given below. Suggest optimum strategies for the two firms and find value of game [10]

		Firm B		
		No Advertising	Medium Advertising	Heavy Advertising
Firm A	No Advertising	10	5	-2
	Medium Advertising	13	12	15
	Heavy Advertising	16	14	10

- b) Solve the following problem using Dual Simplex Method [10]

$$\begin{aligned} \text{Minimize } Z &= 2x_1 + 2x_2 + 4x_3 \\ \text{Subject to } 2x_1 + 3x_2 + 4x_3 &\geq 2 \\ 3x_1 + x_2 + 7x_3 &\leq 3 \\ x_1 + 4x_2 + 6x_3 &\leq 5 \\ x_1, x_2, x_3 &\geq 0 \end{aligned}$$

- Q.5 a) A truck owner finds from his past records that the maintenance cost per year of a truck whose purchase price is Rs. 8000 are given below: [10]

Year:	1	2	3	4	5	6	7	8
Maintenance cost in Rs.:	1000	1300	1700	2200	2900	3800	4800	6000
Resale value in Rs.:	4000	2000	1200	600	500	400	400	400

Determine which time is profitable to replace the truck?

- b) Processing time of six jobs (in hrs) on three machines M1, M2, M3 are given below: [10]

Jobs	1	2	3	4	5	6
M/C M1	3	12	5	2	9	11
M/C M2	8	6	4	6	3	1
M/C M3	13	14	9	12	8	13

Determine the sequence which will minimize the total elapse time. Also find idle time for each machine.

- Q.6 a) Solve using Gomory's cutting plane method [10]

$$\text{Maximize } Z = 7X_1 + 9X_2$$

$$\text{Subject to } -X_1 + 3X_2 \leq 6$$

$$7X_1 + X_2 \leq 35$$

$$x_1, x_2 \geq 0 \text{ and integer}$$

- b) A small assembly plant assembles PCS through 9 interlinked activities. The time duration for which is given below. i) Draw a Network ii) Calculate total float, free float and independent float. [10]

Activity	1-2	1-3	1-4	2-5	3-6	3-7	4-6	5-8	6-9	7-8	8-9
Duration	2	2	1	4	8	5	3	1	5	4	3