

N.B.: 1) Question No.1 is compulsory

2) Answer any three questions from remaining questions

3) Assume data if necessary and specify assumptions clearly

- Q.1** a) Explain Truncation error in short. [5 marks]
 b) Fit a straight line using the following Time Vs Conversion data. [5 marks]

T	5	4	3	2	1
CA	1	2	3	4	5

- c) Solve the boundary value problem $u_t = u_{xx}$ under the conditions $u(0,t) = u(1,t) = 0$ and $\sin \pi x$, $0 \leq x \leq 1$ using Bender Schmidt Method for two time steps. (Take $h=0.2$) [5 marks]
 d) Show progress of bisection method using graphical representation. [5 marks]

- Q.2** a) Using A Solve the boundary value problem $u_t = u_{xx}$ under the conditions $u(0,t) = u(1,t) = 0$ and $\sin \pi x$, $0 \leq x \leq 1$ using Bender Schmidt Method for two time steps. (Take $h=0.2$) [10 marks]

- b) From the following data of variation of fluid temperature with time, obtain dy/dx for $x = 1.4$ by using newton's forward formula. [10 marks]

t Sec	1.4	1.6	1.8	2.0	2.2
T °C	4.0552	4.9530	6.0496	7.3891	9.0250

- Q.3** a) The change in velocity of a moving particle is given by the following equation [10 marks]

$$\frac{dv}{dt} = 0.025v^2 - 5t$$

Where v is in m/s and t is in seconds. If at $t=0$, $v= 5$ m/s. by using Euler's method find $v(1.5)$. (Take step size as 0.25).

- b) Solve $\frac{\partial p}{\partial t} = \frac{\partial^2 p}{\partial y^2}$ subject to the condition $p(y,0)=0$, $p(0,t)=0$, $p(1,t)=100t$ with $k=1/4$, $h=1/2$ for a time step using crank Nicholson method [10 marks]

- Q.4 a)** The temperature of a metal strip was measured at various time intervals during heating and the values are given in the table. If the relationship between temperature T and time t is of the form **[10 marks]**

$$T = be^{t/4} + a$$

Time t (min)	Temperature T (°C)
1	70
2	83
3	100
4	124

Find the temperature at t = 6 minute.

- b)** Solve the following by Gauss-Seidel method **[10 marks]**

$$10x + y + z = 12$$

$$2x + 10y + z = 13$$

$$2x + 2y + 10z = 14$$

- Q.5 a)** Evaluate $\int_0^6 \frac{dx}{1+x^2}$ By using **[10 marks]**

1. Trapezoidal rule
- Simpson's (1/3)rd rule.

- b)** Solve by using LU decomposition method. **[10 marks]**

$$2x + 3y - z = 5$$

$$3x + 2y + z = 10$$

$$x - 5y + 3z = 0$$

- Q.6 a)** Consider a reaction $A \longrightarrow B$ carried out in a batch reactor governed by **[10 marks]**

$$\frac{dCa}{dt} = -kCa$$

The initial conditions are: at t=0, Ca= 1 mol/m³. The rate constant (k) is 1 s⁻¹. Using Runge-Kutta Second order method, determine the concentration of A at 2 s.

(take step size as 1).

[10 Marks]

- b)** Find the root of $f(x) = x^3 - 5x - 7 = 0$, using Secant method correct to three decimal places of decimal point
