

- N. B. :** (1) Question No. 1 is compulsory.  
 (2) Answer any **three** from remaining **five** questions.  
 (3) Assume any data if necessary justify.

1. (a) Check the following systems described by the input output relation is linear or not, stable or not, where  $x(n)$  is the input and  $y(n)$  is the o/p 5  
 (i)  $y(n) = (n+1) e^{x(n)}$   
 (ii)  $y(n) = x(n) x(n-1)$
- (b) Prove the circular time shift property of DFT. 5
- (c) Compute the linear convolution of  $x(n) = (1, 2, 3, -1, 2, -1)$  and  $h(n) = (1, 2, 1)$  using z-transform property only. 5
- (d) Show that the filter with impulse response  $h(n) = (0.075, -0.1592, 0.2251, 0.75, 0.2251, -0.1592, 0.075)$  is a linear phase filter. 5
2. (a) Check whether the signals are periodic or not, if periodic, find the period. 4  
 (i)  $x(n) = e^{j7n}$   
 (ii)  $x(n) = \cos\left(\frac{7\pi}{3}n + \pi/4\right)$
- (b) Find DTFT of the signal  $x(n) = \left(\frac{1}{2}\right)^n u(n)$  4
- (c) Find magnitude and phase response of the system described by the input-output relation  $y(n) = \frac{1}{2} [x(n+1) + x(n) + x(n-1)]$ , where  $y(n)$  is the output and  $x(n)$  is the input. 6
- (d) Find DFT of the signal  $x(n) = (1, 2, 3, 4)$ . From the DFT of  $x(n)$ , find the DFT of the signals of  $x_1(n) = (3, 4, 1, 2)$  and  $x_2(n) = (4, 6, 4, 6)$  using properties of DFT only, not otherwise. 6

3. (a) Develop 8-point, Radix-2 DIF FFT algorithm, draw the flow graph. Find DFT of the signal  $x(n) = (0, 1, 2, 3, 4, 5, 6, 7)$  using the above flow graph. 10
- (b) Using inverse DFT algorithm find  $x(n)$  if  $X(k) = (20, 5.828 - j2.414, 0, -0.172 - j0.414, 0, -0.172 + j0.414, 0, 5.828 + j2.414)$  Draw the flow graph. 10
4. (a) Explain over-lap and add method for finding the linear convolution of long data sequence given  $x(n) = (1, 2, 3, 4, 5, 6, 7, -1, 1, 2, 3, -1, 5, 4, 1, 2)$  and  $h(n) = (1, 2, -1)$  10
- (b) Realise the filter with impulse response. 10

$$H(z) = \frac{1 - \frac{1}{2}z^{-1}}{(1 + \frac{1}{2}z^{-1})(1 + \frac{1}{3}z^{-1})}$$

using direct form-I cascade and parallel form structures.

5. (a) Design a FIR filter with the following desired frequency response. 10

$$H_d(e^{j\omega}) = 0 \quad \text{for } -\frac{\pi}{4} < \omega < \pi/4$$

$$= e^{-j3\omega} \quad \text{for } \frac{\pi}{4} \leq |\omega| \leq \pi$$

Determine the filter coefficients of  $h(n)$  if the Hamming window is used, determine the frequency response  $H(e^{j\omega})$  of the designed filter.

- (b) Design an IIR Butterworth filter that satisfy the following specification using bilinear transformation assume  $T_s = 1$  sec. 10

$$0.9 \leq |H(e^{j\omega})| \leq 1 \quad 0 \leq |\omega| \leq \pi/2$$

$$|H(e^{j\omega})| \leq 0.2 \quad \frac{3\pi}{4} \leq |\omega| \leq \pi$$

6. (a) Convert the analog filter transfer function  $H(s) = \frac{1}{(s+1)(s+2)}$  into a digital filter transfer function using impulse invariant technique assume  $T_s = 1$  sec. 6
- (b) Draw and explain briefly the architecture of any one DSP processor. 7
- (c) Explain briefly the application of BSP in Biomedical engineering. 7