

(3 Hours)

[Total Marks: 80]

- N. B. (i) Question number **one is compulsory**.
 (ii) Answer any **three** questions from the rest.
 (iii) Assume suitable data wherever necessary.

Q.1.a) Explain False position method using graphical representation. (05)

b) Find LU decomposition of $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$ (05)

c) How to use Loops in Python? Explain with examples (05)

d) Using Bender-Schmidt method to solve $\frac{\partial^2 u}{\partial x^2} - 2 \frac{\partial u}{\partial t} = 0$ given $u(0, t) = 0$, $u(4, t) = 0$, $u(x, 0) = x(4-x)$. Assume $h=1$. Find the values of u upto $t=5$ (05)

Q.2.a) Solve the equation $x^3 + x^2 - 1 = 0$ for the positive root by iteration method (Method of successive approximations) (10)

b) Find the positive root of $x = \cos x$ using Newton's Method correct to six decimal places. (10)

Q.3. a) Solve the following equations by Gauss-Elimination Method (08)

$$\begin{aligned} x + 2y + z &= 3 \\ 2x + 3y + 3z &= 10 \\ 3x - y + 2z &= 13 \end{aligned}$$

b) Solve the following equations by Gauss-Jacobi Method (12)

$$\begin{aligned} 10x - 5y - 2z &= 3 \\ 4x - 10y + 3z &= -3 \\ x + 6y + 10z &= -3 \end{aligned}$$

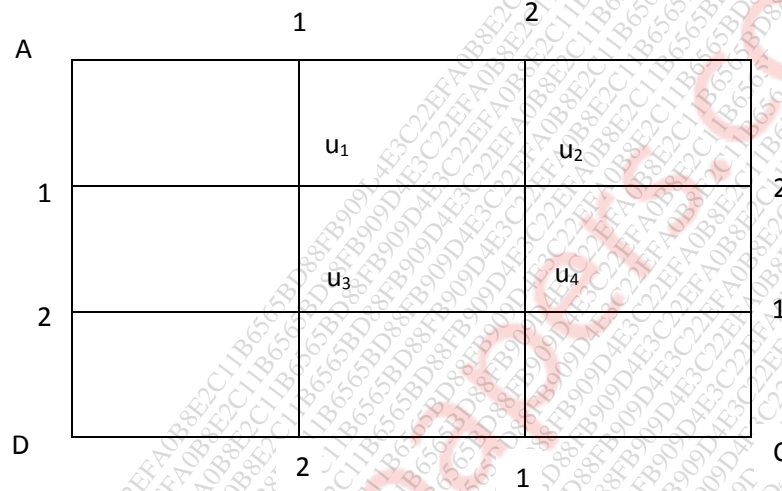
Q.4.a) The change in velocity of a moving particle is given by the following equation (15)

$$\frac{dv}{dt} = 0.025v^2 - 5t$$

Where v is in m/s and t is in seconds. If at $t=0$, $v=5$ m/s, then find the velocity at $t=1.5$ s taking step size as 0.25. Use Euler's Method.

- b) Solve by Crank Nicholson method the equation $u_{xx} = u_t$ subject to the condition $u(x, 0) = 0, u(0, t) = 0$ and $u(1, t) = t$ taking $h=0.25$ for one-time steps. (05)

Q.5.a) Solve $u_{xx} + u_{yy} = 0$ for the following square mesh with boundary conditions as shown below. (12)



- b) Solve $y_{x+2} - 5y_{x+1} + 6y_x = x^2 + x + 1$ (08)

Q.6.a) Using Adam-Bashforth predictor-corrector method find y (0.4) (10)

$$\frac{dy}{dx} = \frac{1}{2}xy, y(0) = 1, y(0.1) = 1.01, y(0.2) = 1.022, y(0.3) = 1.023$$

- b) Compare Newton Raphson and Secant method of finding roots of nonlinear equations (10)