

(3 Hours)

[Total Marks: 80]

**N.B.**

1. Question No. 1 is Compulsory.
2. Attempt any **Three** Questions from remaining **Five** Questions
3. Assume Suitable Data if needed and Justify the Same
4. Figures to the right indicate full marks.

**Q.1**

- a) What are different conditional Loop in Python? Explain any one with example [05]
- b) Use secant method to find the root of equation  $f=4(x-1)^3$  with  $0.4 \leq x \leq 1$ . [05]
- c) Write short note on Successive Substitution Method [05]
- d) Solve  $\frac{dy}{dx} = \frac{1}{2}xy$ ,  $y(0)=1$ ,  $y(0.1)=1.01$ ,  $y(0.2)=1.022$ ,  $y(0.3)=1.023$  and  $h=0.1$  [05]  
find the value of  $y(0.4)_p$  and  $y(0.4)_c$  by Adam-Bashforth Method

**Q.2**

- a) The spherical storage tank containing oil has a diameter of 6 ft. Calculate the height  $h$  to which a dipstick 8 ft long would be wet with oil when immersed in the tank when it contains  $4 \text{ ft}^3$  of oil. The equation that gives the height,  $h$ , of the liquid in the spherical tank for the given volume and radius is given by  $V = \frac{3\pi h^2(3r-h)}{9}$ , Use the Bisection Method to find the height ( $h$ ), to which the dipstick is wet with oil. [10]
- b) Write a short note on one dimensional steady state diffusion with example. [10]

**Q.3**

- a) Solve the following system by LU decomposition [10]

$$\begin{bmatrix} 1 & -1 & 2 \\ 2 & -2 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -8 \\ -20 \\ -2 \end{bmatrix}$$

- b) Solve the following systems of equations by Gauss Jordan Method [10]  
 $5x_1+2x_2+x_3=12$ ,  $x_1+4x_2+2x_3=15$ ,  $x_1+2x_2+5x_3=20$

**Q.4**

- a) if,  $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ ,  $y(0)=1$ ,  $h=0.2$  find  $y(0.4)=?$  [10]

By using runge kutta order 4 method

- b) Calculate the volume of superheated steam at 100atm and 350 °C using the equation [10]

$(P + \frac{a}{v^2})(v - b) = RT$ , Newton Raphson Method, for initial value of v use ideal gas equation.

where,  $a = \frac{27R^2T_c^2}{64P_c}$ ,  $b = \frac{RT_c}{8P_c}$ ,  $T_c=647.11K$ ,  $P_c=220.76 \text{ atm}$ .

### Q.5

- a) Define difference equation and Solve the following Difference Equation [10]

$$y_{n+2} - 3y_{n+1} + 2y_n = 3^n + 7^n$$

- b) Solve the following set of equations using Newton method [10]

$$x_1^2 + x_2^2 - 17 = 0$$

$$2x_1^{1/3} + x_2^{1/2} - 4 = 0$$

Start at a value of  $x = [2.5 \ 0.2]^T$  and show two iterations.

### Q.6

- a) A volume and level in gravity flow tank system is given by following equations, [20]

$$\frac{dV}{dt} = 0.0107h - 0.00205V^2 \quad \frac{dh}{dt} = 0.311 - 0.062V$$

Where,

V in cu. ft and h in ft and time in sec.

The parameters and variables are given as given below.

V= tank volume ,( at t=0, 3.4 cu.ft.)

h= level in tank, (at t=0, 20.5 ft.)

Find the level and volume after 60 Sec using Runge kutta fourth order method.

Use 20 sec as step size.