

AUTO

Q. P. Code: 39287

(Time: 3 Hours)

Max. Marks: 80

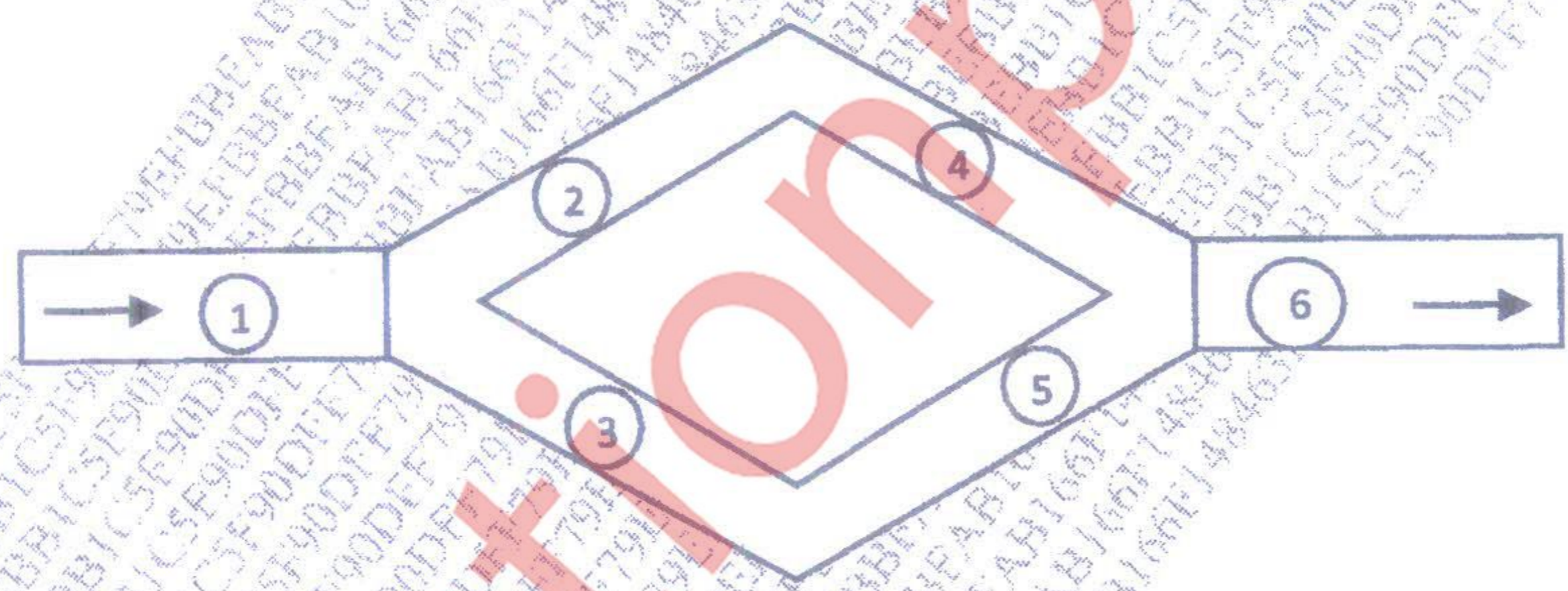
Note:

- 1. Question 1 is Compulsory
- 2. Solve any three from remaining five
- 3. Figures to right indicate full marks
- 4. Assume suitable data if necessary

- Q.1 a) Discuss the different types of coordinate systems used in finite element method of analysis. 20
- b) What is the significance of shape functions?
- c) Prove that the strain for a three node triangular element is constant.
- d) Explain Weak & Non Weak form method used in FEA.

- Q.2 a) Solve following differential equation by Galerkin method. 10
- $$-\frac{d^2y}{dx^2} - 9y + 2x^2 = 0; 0 \leq x \leq 1$$
- Given Boundary Conditions are: $y = 0$ at $x = 0$, $\frac{dy}{dx} = 1$ at $x = 1$
- Find values for $y(0.5)$ & $y(0.7)$

- b) For the fluid network shown in figure write the global matrix equation. 10



| Element No. | 1 | 2 | 3 | 4 | 5 | 6 |
|-------------|----|-----|-----|----|----|----|
| L cm | 70 | 50 | 50 | 70 | 60 | 55 |
| d cm | 10 | 7.5 | 7.5 | 5 | 8 | 5 |

Pipe resistance is given by R^e

$$R^e = \frac{128\mu h_e}{\pi d_e^4}$$

- Q.3 a) Derive the shape function for a rectangular element in local coordinate system. 10

- b) The governing differential equation for the steady state one dimensional conduction heat transfer with convection heat loss from lateral surfaces is given by 10

$$k \frac{d^2T}{dx^2} + q = \left(\frac{P}{A_c}\right) h(T - T_\infty)$$

where

K = coefficient of thermal conductivity of the material,

T = Temperature

q = internal heat source per unit volume

P = Perimeter

A_c = the cross-sectional area,

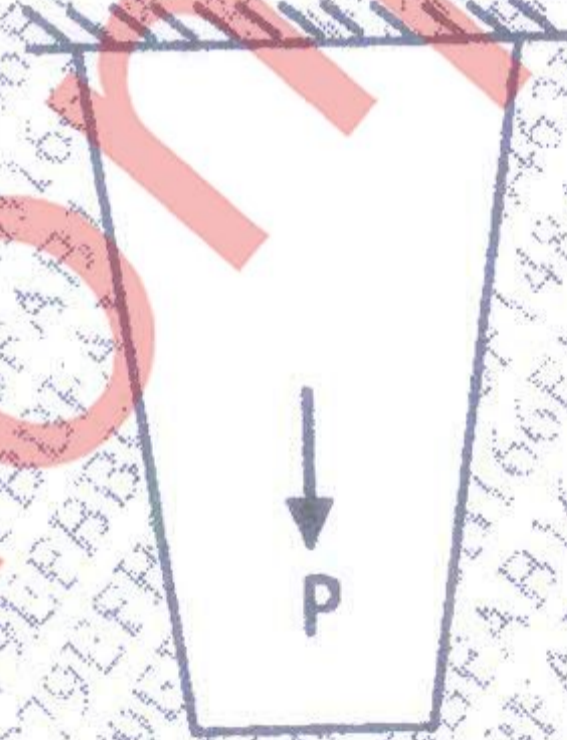
h = convective heat transfer coefficient, and

T_∞ = Ambient Temperature

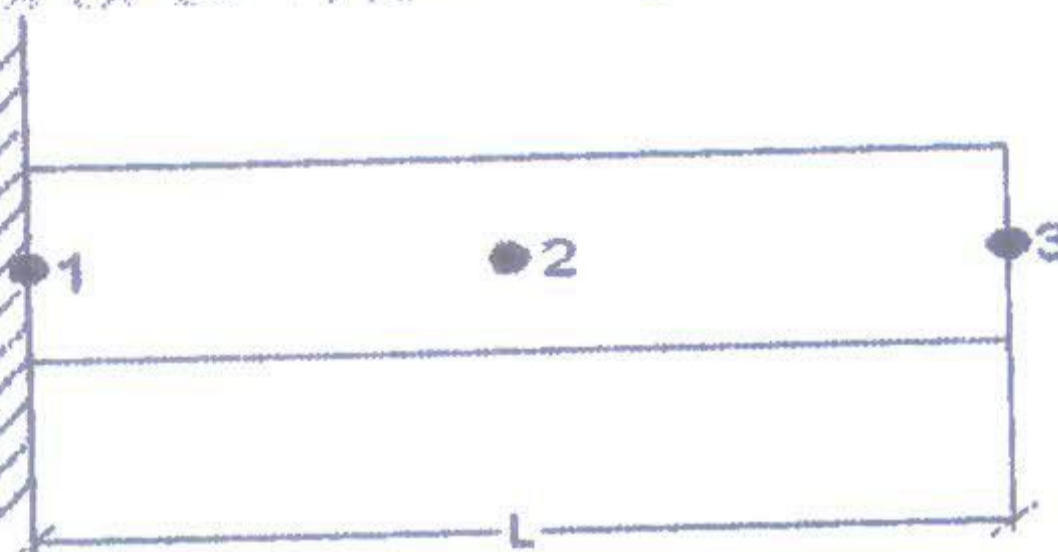
Develop the finite element formulation for linear element. Use Rayleigh Ritz method, mapped over general element. Derive relevant element level matrix equation.

Q.4

- a) A tapered thin plate made of steel ($E = 200 \text{ GPa}$, $\rho = 7800 \text{ kg/m}^3$) has a length of 500 mm and a thickness of 20mm. Its width is 180 mm at the fixed end and 80mm at the free end. In addition to its self-weight, it is subjected to a point load P of 50kN at a distance of 300mm from the fixed end. Model the plate with two spar elements and determine the nodal displacements and stresses in each element. 10

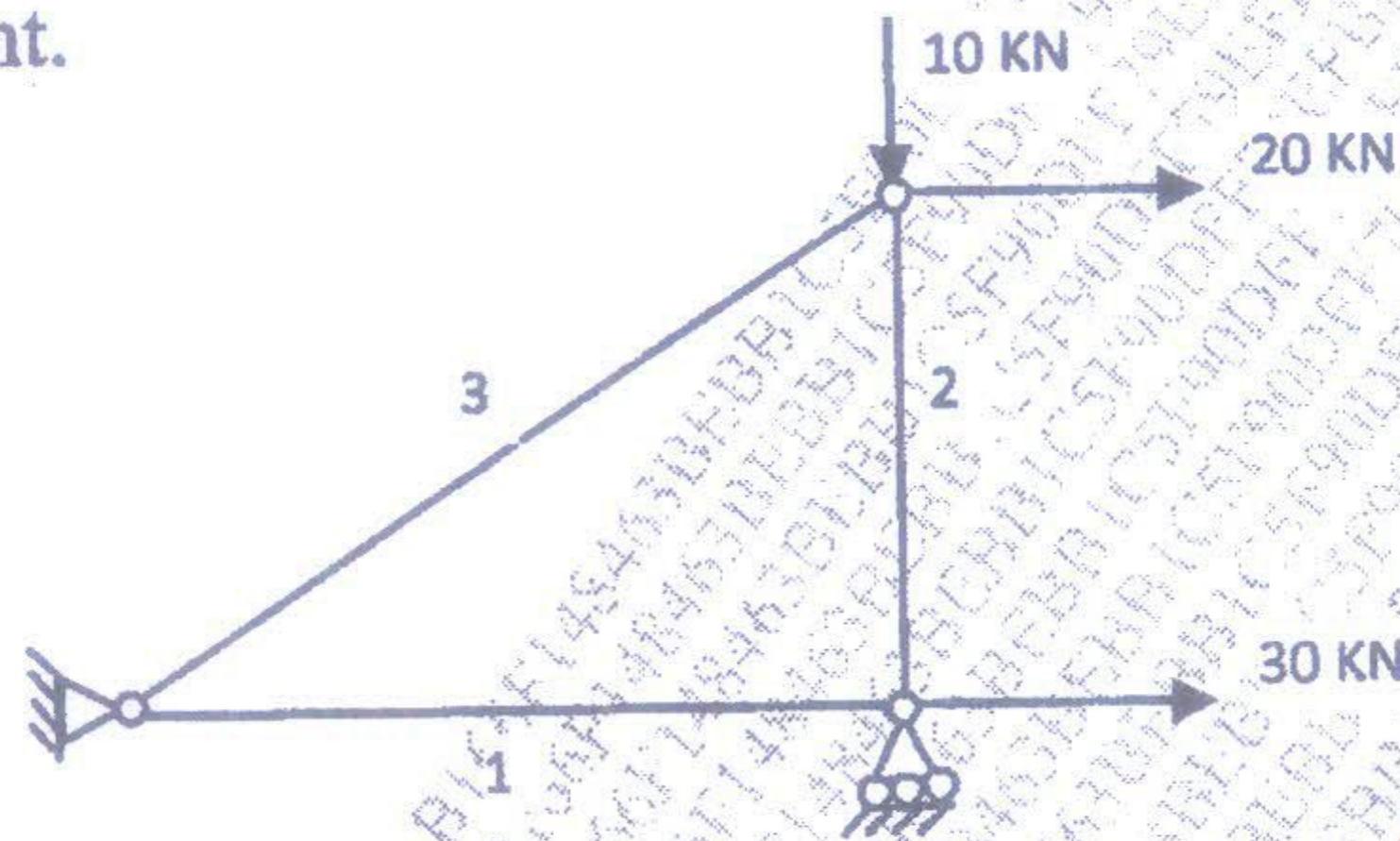


- b) A uniform cross section bar as shown below has a length $L=1 \text{ m}$ and made up of a material having $E=2 \times 10^{11} \text{ N/m}^2$ & $\rho = 7800 \text{ kg/m}^3$. Estimate the natural frequencies of axial vibration of the bar using a two element mesh. $A= 30 \times 10^{-6} \text{ m}^2$. Compare the natural frequencies with exact frequencies. 10

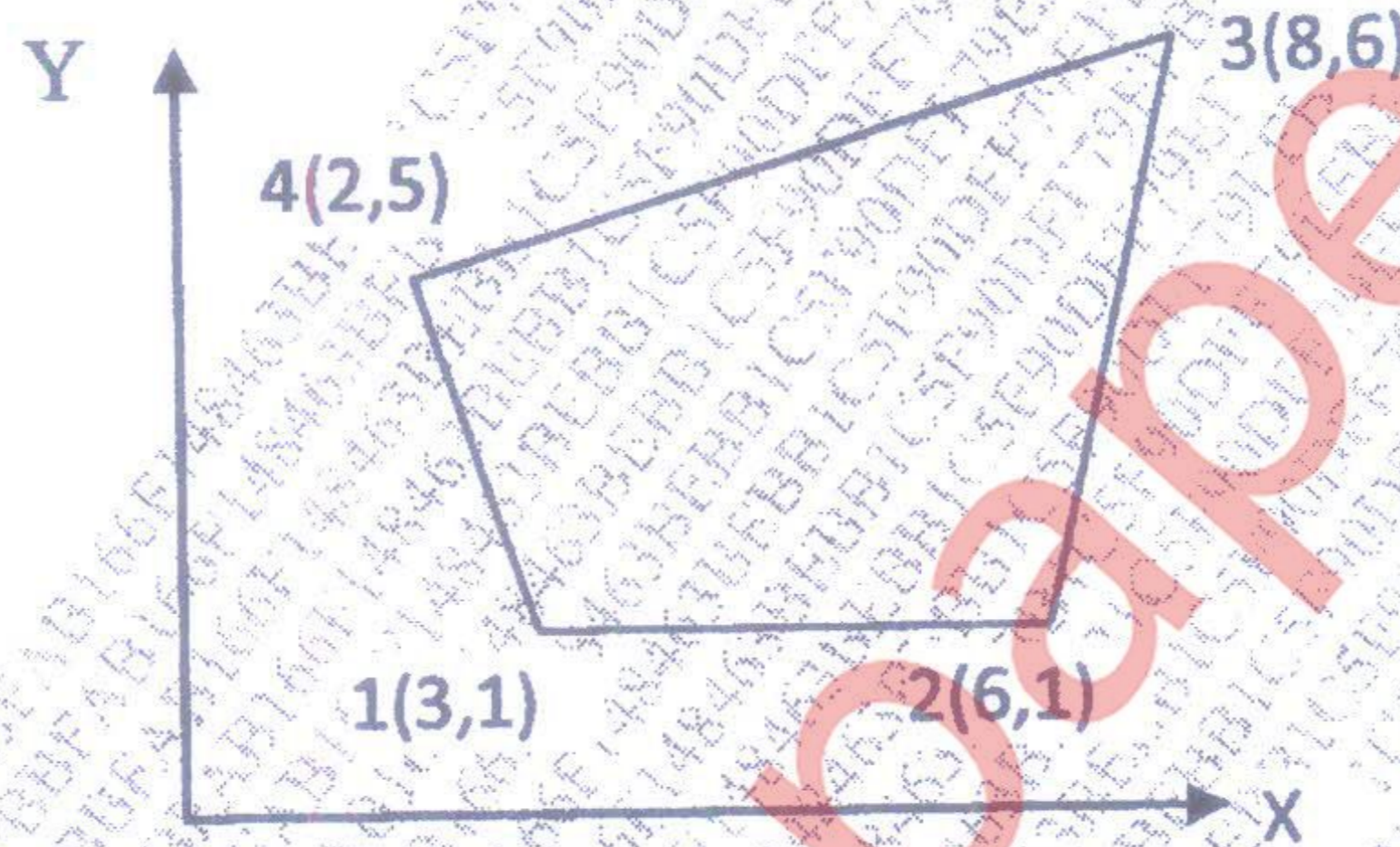


Q.5

- a) A three bar truss is subjected to loading as shown. The modulus of elasticity for the bar material is 300 GPa. The cross sectional area of each bar used for truss is 300 mm². The length of the elements are $l_1=800\text{mm}$, $l_2=600\text{mm}$ and $l_3=1000\text{mm}$. Determine the nodal displacements and stresses in each element. 10

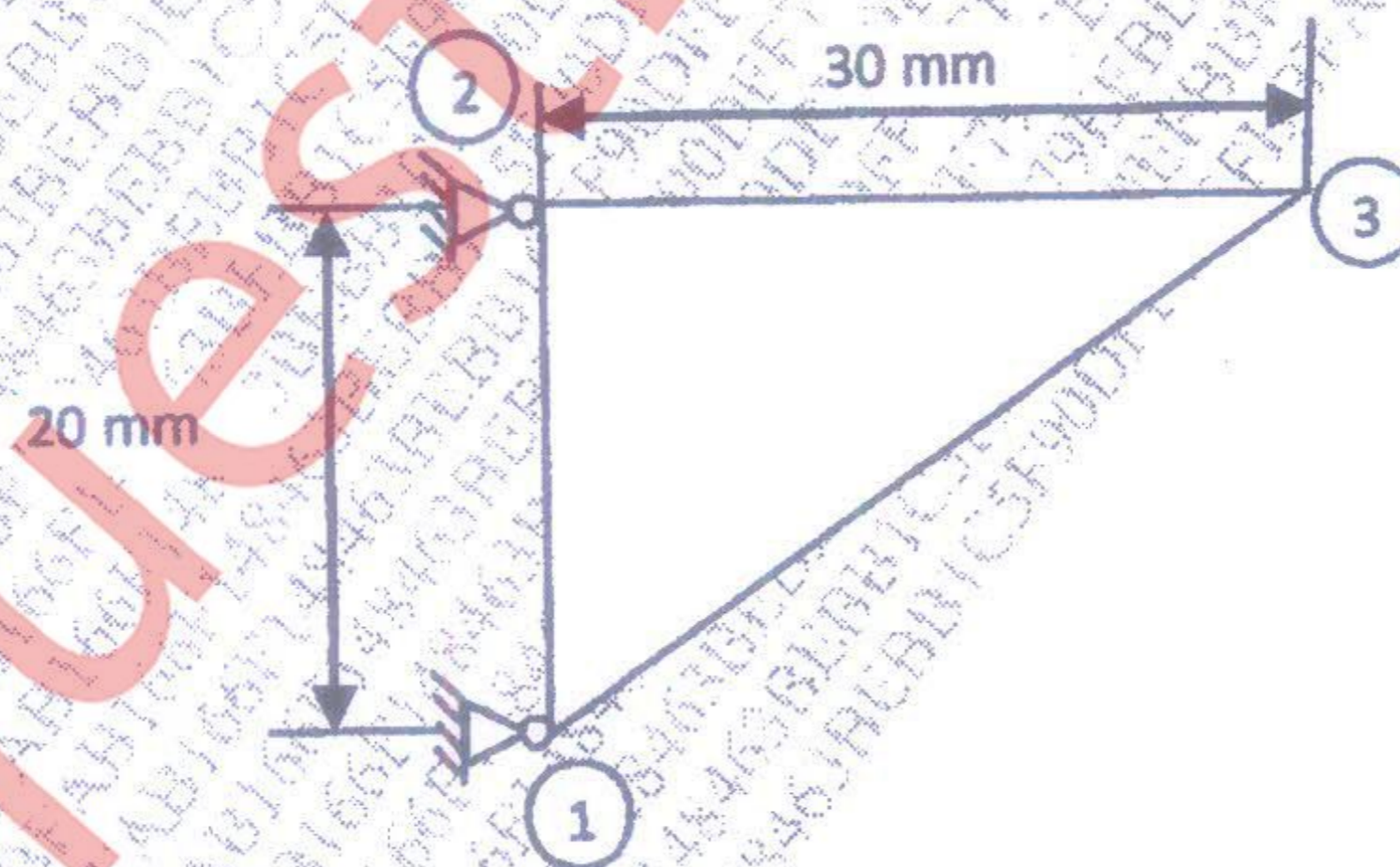


- b) For the iso-parametric quadrilateral elements shown in figure determine cartesian coordinates of the point P which has local coordinates ($\xi=0.9125$ and $\eta = 0.2106$) 10



Q.6

- a) A triangular plate ($E = 210 \text{ GPa}$, $\nu = 0.3$) of thickness 10 mm is as shown in figure. Node 1 and 2 are fixed and the displacements at node 3 are $1.95 \times 10^{-4} \text{ mm}$ and $-1.114 \times 10^{-3} \text{ mm}$ in x and y direction respectively. Determine the element stresses. 12



- b) Obtain the strain-nodal displacement relationship for one dimensional linear element. 08