

Note:

1. Question 1 is Compulsory
2. Solve any three from remaining five
3. Figures to right indicate full marks
4. Assume suitable data if necessary

Q.1 Attempt any four

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- a) Write element matrix equation in the following fields explaining each term:
 - i. 1D steady state, heat transfer by conduction
 - ii. Torsion Analysis
- b) Prove that linear triangular element is CST element.
- c) Explain different types of Boundary conditions with examples.
- d) Explain plane stress and plane strain conditions with examples.
- e) What do you mean by consistent mass matrix and lumped mass matrix. Give suitable mathematical expression?

Q.2

- a) Solve the following differential equation using Method of least square and Galerkin method.

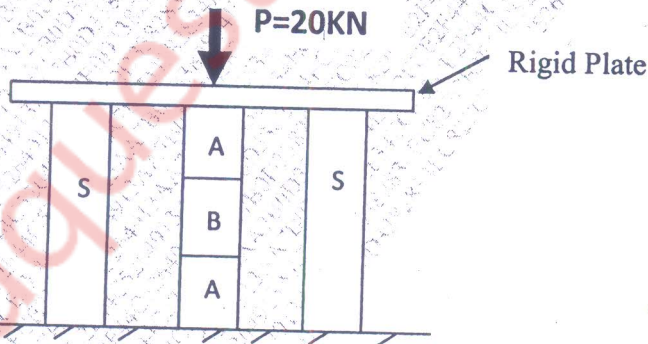
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$$\frac{d^2y}{dx^2} - 10x^2 = 5; 0 \leq y \leq 1; y(0) = 0, y(1) = 0$$

Compare answer with exact solution at $x = 0.5$

- b) Find the displacement at nodes and stresses over each element.

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| PROPERTIES | STEEL (S) | ALUMINIUM (A) | BRASS (B) |
|-----------------------|-----------------|-----------------|-------------------|
| AREA, mm ² | 200 | 370 | 370 |
| E, N/mm ² | 2×10^5 | 7×10^4 | 8.8×10^4 |
| Length, mm | 1000 | 350 | 300 |

- Q.3 a) A copper fin of diameter 2 cm, length 6 cm and thermal conductivity is 100 W/m °C and is exposed to ambient air at 30 °C with a heat transfer coefficient 25 W/m² °C. If one end of the fin is maintained at temperature 500 °C and other end is at 200 °C. Solve the following differential equation for obtaining the temperature distribution over the length of a fin. 14

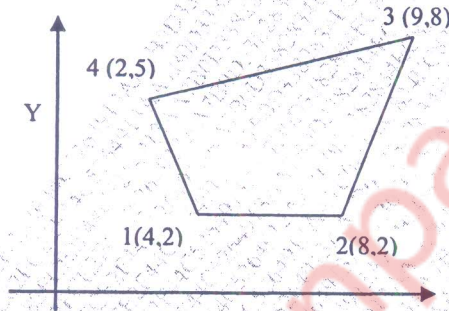
$$kA \frac{d^2\theta}{dx^2} - hp\theta = 0$$

$\theta =$ Temperature difference $= T_x - T_a$.

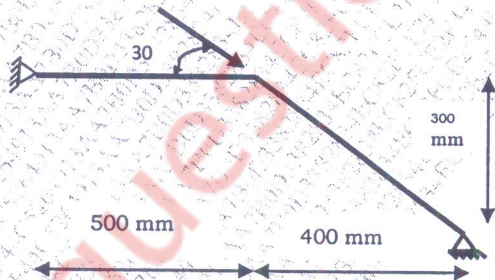
Use Rayleigh-Ritz method, mapped over general element, taking Lagrange's linear shape functions and three linear elements.

Write all the steps clearly. Compare your answer with exact at $x = 2,4$ cm

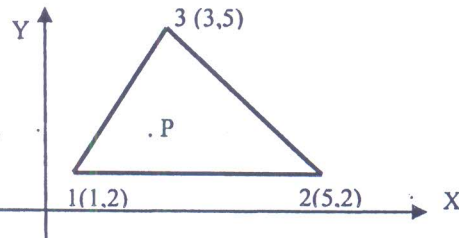
- b) For the iso parametric quadrilateral element shown in figure. Determine Cartesian coordinates of point P which has local coordinates $(\xi, \eta) = (0.57735, 0.57735)$. 6



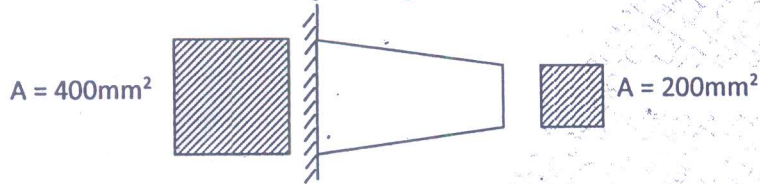
- Q.4 a) Compute the stress developed in the members of the truss shown in figure. $E = 200$ GPa. Area of the each member is 200 mm². 10



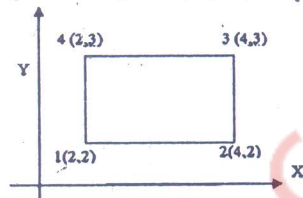
- b) The nodal coordinate of the triangular element are as shown in figure. Take the nodal displacement vector $Q^T = [2.0, 1.0, 3.0, 2.0, 5.0, 3.0]$ in mm. Obtain the displacement at the interior point P whose x and y coordinate is (1.5). 10



- Q.5 a) Evaluate the natural frequencies for the bar with varying cross sections shown in figure. $L = 200$ mm, $E = 200$ GPa and $\rho = 8000$ kg/m³. Consider two elements of equal lengths. 10



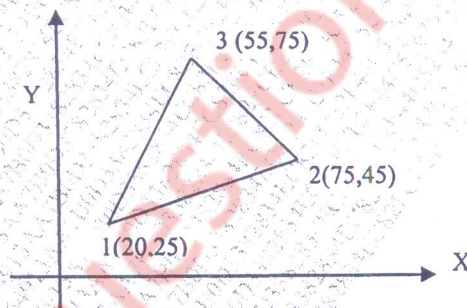
- b) Quadrilateral element is shown in figure. The temperatures at the nodes are $T_1=100^\circ\text{C}$, $T_2=60^\circ\text{C}$, $T_3=50^\circ\text{C}$ and $T_4=90^\circ\text{C}$ respectively. Determine the temperature at a point P (2.5, 2.5)



- Q.6 a) A CST element is shown in figure. The modulus of elasticity and Poisson's ratio for plate material are 70×10^3 N/mm² and 0.3 respectively. Upon loading of the plate, the nodal deflections were found to be in x and y direction respectively as $u_1 = 0.01$ mm and $v_1 = -0.04$ mm, $u_2 = 0.03$ mm and $v_2 = -0.02$ mm, $u_3 = -0.02$ mm and $v_3 = -0.04$ mm. 12

Determine :

- i. The Jacobian for (x,y) - (ξ,η) transformation
- ii. The strain-displacement relation matrix
- iii. The stress in plate



- b) Explain Convergence criteria. What do you understand by h & p method of Finite Element Analysis? 08