

(2 ½ Hours)

[Total Marks: 75]

- N.B.** 1) All questions are **compulsory**.  
 2) **Figures** to the **right** indicate marks.  
 3) **Draw** suitable **diagrams** and illustrations **wherever necessary**.  
 4) **Mixing** of sub-questions is **not allowed**.

**Q. 1 Attempt All the Questions****A. Choose the correct alternative**

(5M)

- i. The grammar  $G = (\{S\}, \{a, b\}, P, S)$  where  $P$  consists of  
 $S \rightarrow aSbb, S \rightarrow aab$   
 generates the language \_\_\_\_\_  
 a)  $a^m b^n \mid m > n, m, n \geq 1$                       b)  $a^n b^{2n} \mid n \geq 1$   
 c)  $a^m b^n \mid m < n, m, n \geq 1$                       d) none of these
- ii. The regular expression  $(P+Q)^*$  is equal to  
 a)  $(P^*+Q^*)^*$     b)  $(P^*Q^*)^+$   
 c)  $(P^*+Q^*)^+$     d)  $(P^*+Q^*)$
- iii. Pumping lemma for context-free languages are used to prove that certain languages are not context-free.  
 a) True    b) False
- iv. PDA stands for \_\_\_\_\_  
 a) pull down automata                                      b) push direct automata  
 c) push down automata                                      d) pull direct automata
- v. In \_\_\_\_\_ machine, the output function  $Z(t)$  depends only on the present state and is independent of the current input.  
 a) Moore    b) Mealy  
 c) Both a and b    d) None of these

**B. Fill in the blanks (Choose correct one from the pool)**

(5M)

(type 2, type 1, one, three, not regular, regular,  $a^+$ ,  $a^*$ , initial, final)

- i. The regular expression  $aa^*$  is same as \_\_\_\_\_.
- ii. A finite automaton can have more than one \_\_\_\_\_ state.
- iii. The language  $L = \{a^p \mid p \text{ is a prime}\}$  is \_\_\_\_\_.
- iv. Regular expression  $(aaa)^*$  denotes the string  $x$  whose length is divisible by \_\_\_\_\_
- v. Context sensitive grammar is also known as \_\_\_\_\_ grammar

**C. Explain the following terms in one or two lines**

(5M)

- i. Non deterministic finite automaton  
 ii. Regular expression  
 iii. Acceptance by PDA  
 iv. Derivation tree  
 v. Decidable languages

**Q.2 Attempt the following: (Any THREE) (15M)**

- What is finite automaton? Briefly explain with suitable example the acceptability of a string by a finite automaton.
- Compare between Mealy and Moore models.
- Construct DFA accepting all strings  $w$  over  $\{a, b\}$  such that the number of  $a$ 's in  $w$  is  $3 \pmod 4$ .
- Define Grammar. Also explain what is a language generated by a grammar. Give examples.
- Compare between deterministic and non-deterministic finite automaton. Give suitable examples.
- Write a note on operations on Languages.

**Q.3 Attempt the following: (Any THREE) (15M)**

- Prove that  $(a+b)^* = a^*(ba^*)^*$ .
- Explain with suitable example the leftmost derivation and rightmost derivations. Give example.
- What is meant by ambiguity in context free grammar? Give example to explain the concept.
- Write a note on Chomsky Normal Form.
- State and prove pumping lemma for regular sets.
- Draw the transition diagram for the expressions
  - $a^*+ba^*$
  - $a^*b+ba^*$

**Q.4 Attempt the following: (Any THREE) (15M)**

- Briefly explain the structure and operation of Push down automata.
- Write a note on representation of Turing machine.
- Design a Turing machine to recognize all strings consisting of even number of  $a$ 's
- Write a note on model of Linear Bounded Automaton.
- Write a note on nondeterministic Turing machine.
- Write a note on properties of recursive languages.

**Q.5 Attempt the following: (Any THREE) (15M)**

- Briefly explain with example the steps of construction of minimum automaton.
- Consider the grammar  $G$  given by
 
$$S \rightarrow 0SA_12 \quad S \rightarrow 012 \quad 2A_1 \rightarrow A_12 \quad 1A_1 \rightarrow 11$$
 Test whether (a)  $00112 \in L(G)$  (b)  $001122 \in L(G)$
- Construct a DFA with reduced states equivalent to the regular expression  $10 + (0+11)0^*1$
- Design a Turing Machine that accepts  $\{a^n 1^n \mid n \geq 1\}$
- Write a note on Universal Turing machines
- Briefly outline the halting problem of Turing machine.