



QP Code : 5106

Time :3 hours

( Revised course )

Total marks :80

- N.B : (1) Question No.1 is compulsory.  
 (2) Answer any three questions from remaining.  
 (3) Assume suitable data if necessary.

Evaluate

1. (a)  $\int_0^{\infty} e^{-t} \left( \frac{\cos 3t - \cos 2t}{t} \right) dt$  05
- (b) Obtain the Fourier Series expression for  $f(x) = 2x - 1$  in  $(0,3)$  05
- (c) Find the value of 'p' such that the function  $f(z) = \frac{1}{2} \log(x^2 + y^2) + i \tan^{-1} \left( \frac{py}{x} \right)$  is analytic. 05
- (d) If  $\vec{F} = (y \sin z - \sin x)\hat{i} + (x \sin z + 2yz)\hat{j} + (xy \cos z + y^2)\hat{k}$ . Show that  $\vec{F}$  is irrotational. Also find its scalar potential. 05
2. (a) Solve the differential equation using Laplace Transform  $\frac{d^2y}{dt^2} + 2\frac{dy}{dt} + y = 3te^{-t}$ , given  $y(0)=4$  and  $y'(0)=2$  06
- (b) Prove that  $J_4(x) = \left( \frac{48}{x^3} - \frac{8}{x} \right) J_1(x) - \left( \frac{24}{x^2} - 1 \right) J_0(x)$  06
- (c) i) In what direction is the directional derivative of  $\phi = x^2y^2z^4$  at  $(3,-1,-2)$  maximum. Find its magnitude. 08  
 ii) If  $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$   
 Prove that  $\nabla r^n = nr^{n-2}\vec{r}$

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3. (a) Obtain the Fourier Series expansion for the function

$$f(x) = 1 + \frac{2x}{\pi}, -\pi \leq x \leq 0$$

06

$$= 1 - \frac{2x}{\pi}, 0 \leq x \leq \pi$$

- (b) Find an analytic function  $f(z) = u + iv$  where.

06

$$u - v = \frac{x - y}{x^2 + 4xy + y^2}$$

- (c) Find Laplace transform of

08

i)  $\cosh t \int_0^t e^u \sinh u$

ii)  $t\sqrt{1 + \sin t}$

4. (a) Obtain the complex form of Fourier series for  
 $f(x) = e^{ax}$  in  $(-L, L)$

06

- (b) Prove that

06

$$\int x^4 J_1(x) dx = x^4 J_1(x) - 2x^3 J_2(x) + c$$

- (c) Find

08

i)  $L^{-1} \left[ \frac{2s-1}{s^2+4s+29} \right]$

ii)  $L^{-1} \left[ \cot^{-1} \left( \frac{s-3}{2} \right) \right]$

5. (a) Find the Bi-linear Transformation which maps the points  
 $1, i, -i$  of  $z$  plane onto  $0, 1, \infty$  of  $w$ -plane

06

- (b) Using Convolution theorem find

06

$$L^{-1} \left[ \frac{s^2}{(s^2+4)^2} \right]$$

(c) Verify Green's Theorem for  $\int_C \vec{F} \cdot d\vec{r}$  where 08

$\vec{F} = (x^2 - y^2)\hat{i} + (x + y)\hat{j}$  and C is the triangle with vertices (0,0), (1,1) and (2,1)

6. (a) Obtain half range sine series for 06  
 $f(x) = x, 0 \leq x \leq 2$

$$= 4 - x, 2 \leq x \leq 4$$

(b) Prove that the transformation 06  
 $w = \frac{1}{z+i}$  transforms the real axis of the z-plane into a circle in the w-plane.

(c) i) Use Stoke's Theorem to evaluate  $\int_C \vec{F} \cdot d\vec{r}$  where 08

$\vec{F} = (x^2 - y^2)\hat{i} + 2xy\hat{j}$  and C is the rectangle in the plane  $z=0$ , bounded by  $x=0, y=0, x=a$  and  $y=b$ .

ii) Use Gauss Divergence Theorem to evaluate  
 $\iint_S \vec{F} \cdot \hat{n} ds$  where  $\vec{F} = 4x\hat{i} + 3y\hat{j} - 2z\hat{k}$  and S is the surface bounded by  $x=0, y=0, z=0$  and  $2x+2y+z=4$



Course: S.E. (SEM - III) (REV.-2012) (CBSGS) 2015

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Correction:

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Corrections in Question paper code :5106

Q.1 a) Evaluate

$$\int_0^{\infty} e^{-t} \left( \frac{\cos 3t - \cos 2t}{t} \right) dt$$

Q.2.(a)  $\frac{d^2 y}{dt^2} + 2 \frac{dy}{dt} + y = 3te^{-t}$

Q.3 c i)

$$\cosh t \int_0^t e^u \sinh u du$$

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