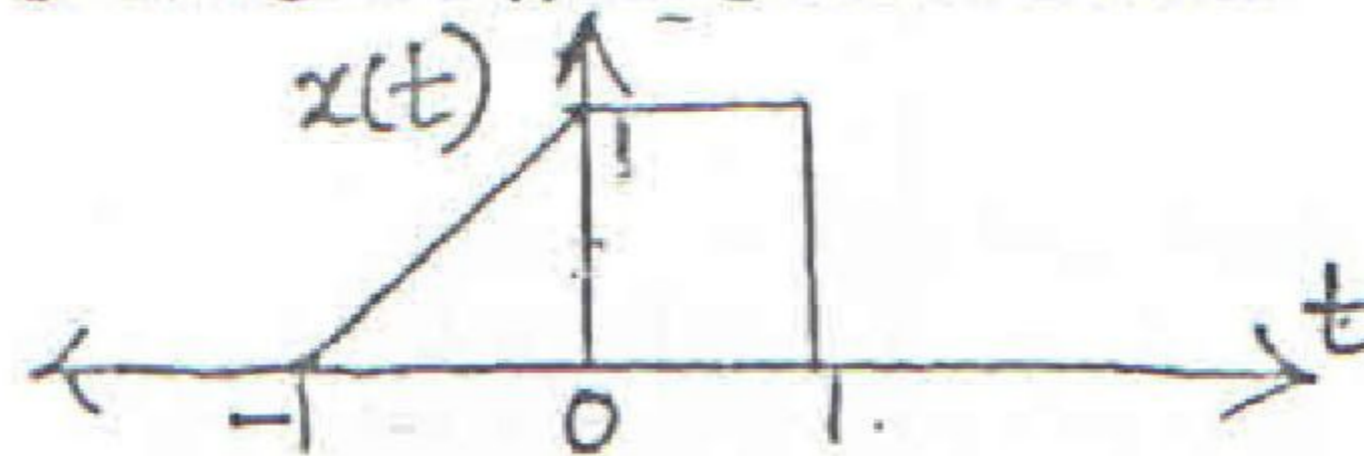


[3 Hours]

- N: B 1) Q1 is compulsory.  
 2) Attempt any three questions from remaining questions  
 3) Assume suitable data wherever required.
- Q1) a) State and prove differentiation property of z-transform.  
 b) Express the given signal  $x(t)$  using basic functions.



[5\*4]

- c) Determine the stability and causality of the system described by

$$H(z) = \frac{1}{1-0.5z^{-1}} + \frac{1}{1-2z^{-1}} \text{ for ROC } 0.5 < |z| < 2$$

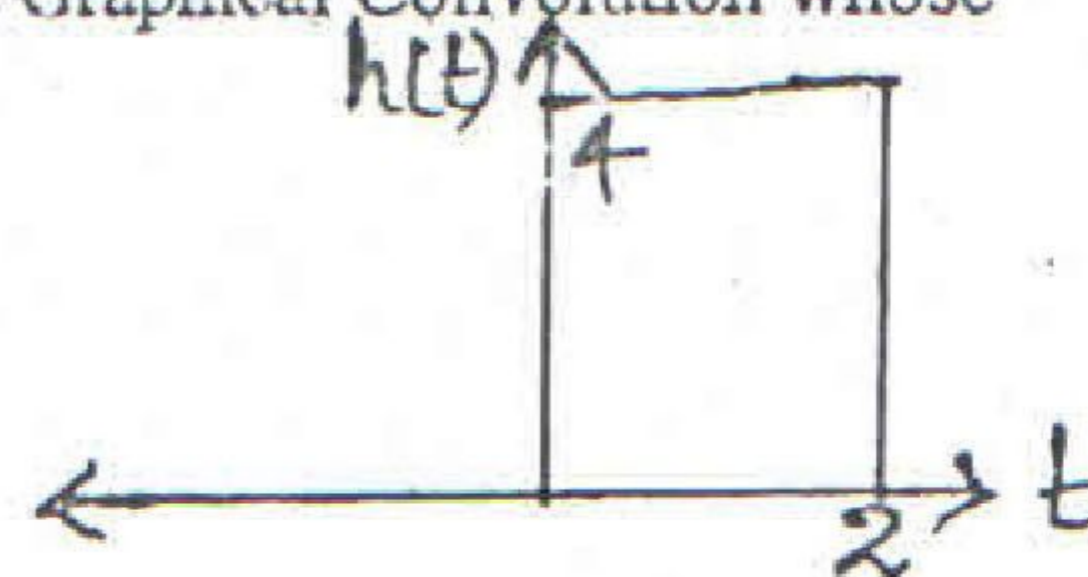
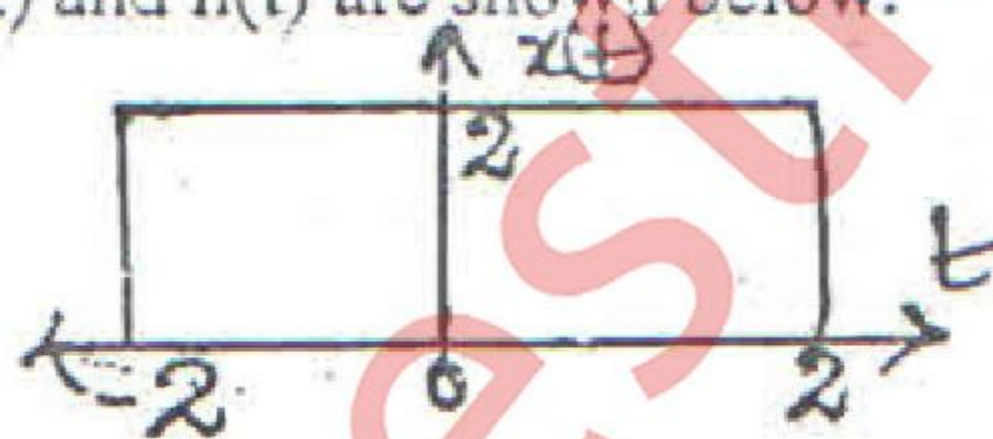
- d) Check the stability and Time invariance property of the system  $y[n] = x[-n]$

- Q2) a) Find the even and odd components of  $x[n] = \{-1, 7, -2, 3, -7, 6\}$  [05]  
 b) Find the initial value and final value of

$$X(z) = \frac{z}{4z^2 - 5z - 1} \text{ ROC } |z| > 1 \quad [05]$$

- c) Find the response  $y(t)$  of an LTI system by Graphical Convolution whose

$x(t)$  and  $h(t)$  are shown below:



[10]

- Q3) a) What do you mean by ROC? Mention the significance. Find the ROC of infinite duration Left sided signal.  
 b) Find the Fourier transform of  $x(t) = e^{-3t} u(t-2)$  [5\*4]  
 c) Check whether the given signal  $x(t) = \sin^2 \omega_0 t$  is power signal or not.  
 d) Obtain the z-transform of  $x(n) = (n-3) u(n)$

[TURN OVER]

- Q4 a) Find the phase and magnitude response of the system  $h(n) = [1, -1/2]$  (10M)
- b) A causal LTI system is described by the difference equation. (10M)
- $$y(n) - 3/4y(n-1) + 1/8y(n-2) = u(n) + u(n-1)$$
- Find the forced response of the system due to step input.
- Q5 a) Find the Z transform of the given signal  $x(n) = \begin{cases} 1 & n \geq 0 \\ 3^n & n < 0 \end{cases}$  (10M)
- b) An discrete time LTI system governed by the difference equation: (10M)
- $$Y(n) = x(n) + 0.8x(n-1) + 0.8x(n-2) - 0.49y(n-2)$$
- Determine the transfer function. Sketch the pole zero plot on the Z plane.
- Q6 a) An 8 point sequence is given by  $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$ . Compute 8 point DFT of  $x(n)$  by radix -2 DIT - FFT method. (10M)
- b) Perform the circular convolution using DFT.  $X_1(n) = \{2, 1, 2, 1\}$   $X_2(n) = \{1, 2, 3, 4\}$  (10M)