

Q.P. Code: 24009

(3 Hours)

Total Marks: 80

Note:

- Question 1 is **compulsory**.
- Solve ant **three** questions from questions no. 2 to 6.
- Assume necessary data wherever necessary.

Q1 Answer the following questions 20

- What do you mean by an error? Discuss propagation of error with suitable example.
- Write the algorithm for golden section search method.
- What is the need for optimization? Explain constrained optimization.
- What do you mean by bracketing method? Discuss the methods with suitable example.

Q2 a) Solve the equation  $y'' = 8 + 6xy'$  using 4<sup>th</sup> order RK method at  $x=0.2$  correct up to 4 decimal places. Initial conditions are  $x=0, y=0, y'=0.1$ . The step size  $h=0.2$  10Q2 b) Solve the equation  $\frac{dy}{dx} = 2x + y$  using Milne's Predictor-Corrector method. Find  $y$  at  $x=0.4$  and  $x=0.5$  with step size of 0.1. Given that  $y(0) = 0.2, y(0.1) = 0.2313, y(0.2) = 0.2870, y(0.3) = 0.3696$ . 10Q3 a) Write the algorithm for Newton's divided difference interpolation. For the following data, find  $y$  at  $x=4.8$ . 10

x	4	5	7	10	11	13
y	48	100	294	900	1210	2028

Q3 b) Minimize  $Z = 2x_1^2 + x_2^2$  5  
subjected to  $x_1 + x_2 = 1$   
 $x_1, x_2 \geq 0$   
Using Lagrange's multiplier method.Q3 c) What are the basic requirements of Linear programming? Discuss the various terms used in LPP. 5

- Q4 a) Solve the following system of equations using LU method. What are the advantages of this method? 10

$$\begin{aligned} x + y + z &= 1 \\ 4x + 3y - z &= 6 \\ 3x + 5y + 3z &= 4 \end{aligned}$$

- Q4 b) Solve using Secant method to obtain root of equation  $xe^x - \cos 3x - 0.51 = 0$ . Do four iterations. Write the algorithm for the same. 10

- Q5 a) Minimize cost  $Z = 400x_1 + 800x_2$   
 subject to  $6x_1 + 2x_2 \geq 12$   
 $2x_1 + 2x_2 \geq 8$   
 $4x_1 + 12x_2 \geq 24$   
 $x_1, x_2 \geq 0$  using graphical method. 10

- Q5 b) Determine root of equation  $f(x) = 0.51x - \sin x$  using Newton Raphson method for three iterations. 10

- Q6 a) Using Simplex method solve 10  
 $Max Z = 3x_1 + 2x_2$   
 subjected to  $x_1 + x_2 \leq 4$   
 $x_1 - x_2 \leq 2$   
 $x_1, x_2 \geq 0$

- Q6 b) Solve the equation  $dy/dx = 1 + xy^2$  with  $y(0) = 0.2$  using Adam's Bashforth method. Determine  $y$  at  $x=0.5$  with a step size of 0.1. 10

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