

(3 Hours)

[Total Marks: 80]

N.B.:

- Question No. 1 is compulsory.
- Answer any **three** from the remaining five questions.
- Assume suitable data if necessary and justify the same.
- Figures to the right indicate the marks.

1 Each question carry five marks

20

- What is significant figures? What are the rules on determining how many significant figures are in a number? Identify the number of significant figures in 0.00800.
- Compare Graphical and simplex method to solve a linear programming problem. How the multiple solution condition can be identified from the graphical and the simplex method?
- Given three data points (1,6) and (3,28), (5,35). Estimate 'x' at y=20 using Lagrange's method
- Given $\frac{dy}{dx} = x^2(1+y)$ and $y(1) = 1$, $y(1.1) = 1.233$, $y(1.2) = 1.548$, $y(1.3) = 1.979$, evaluate $y(1.4)$ till the error is less than 1% using Adams-Bashforth method.

- 2 a Integrate the following set of differential equations using three approximations of Picard's method. Calculate the values of y and z at x=1 by assuming that at x=0, y=4 and z=6.

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$$\frac{dy}{dx} = -0.5y; \quad \frac{dz}{dx} = 4 - 0.3z - 0.1y$$

- b Write the algorithm to find the root of an equation using secant and false position method. Compare the selection of guesses in each iteration of secant and false position method.

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- 3 a What is meant by curve fitting? Compare least square fitting technique with interpolation technique. Using Newton's Divided difference method of order '3' find 'y' at x = 2.5 from the following data with maximum accuracy.

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x	0	1	1.5	3	3.5
y	1	0.5	-1	7	8.2

- b A series RL circuit with $R = 50 \Omega$ and $L = 10 \text{ H}$ has a voltage $V = 150 \sin 1000t$ is applied at $t = 0$ by the closing of a switch. The differential equation to represent the system is given as $Ri + L \frac{di}{dt} = V$. Find the current at $t = 1 \text{ sec}$ taking $h=0.5$ using fourth order Runge Kutta method.

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- 4 a Obtain the roots of following systems of equations using N-R method $f(x,y)=x^2+xy-10$ and $g(x,y)=y+3xy^2-57$ with the initial guesses as $x_0=1.5$ and $y_0=3.5$. Do only two iterations. 10
- b Solve the following LP problem using Simplex method. 10
Maximize $Z = 3x + 2y$
subject to: $2x + y \leq 18$
 $2x + 3y \leq 42$
 $3x + y \leq 24$
 $x \geq 0, y \geq 0$
- 5 a What is LU decomposition? What is the advantage of solving a set of linear algebraic equations using LU decomposition? Calculate the LU decomposition of 10
- $$A = \begin{bmatrix} 1 & 3 & 2 \\ 2 & 8 & 5 \\ 1 & 11 & 4 \end{bmatrix}$$
- b A firm is engaged in producing two products, A and B. Each unit of product A requires 2 kg of raw material and 4 labour hours for processing, whereas each unit of B requires 3 kg of raw materials and 3 labour hours for the same type. Every week, the firm has an availability of 60 kg of raw material and 96 labour hours. One unit of product A sold yields Rs.40 and one unit of product B sold gives Rs.35 as profit. Formulate this as a Linear Programming Problem and determine how many units of each of the products should be produced per week so that the firm can earn maximum profit using graphical method. 10
- 6 a What are the different type of errors in numerical computation? How these errors are propagated under addition and multiplication? 10
- b Explain suitable techniques to solve the following optimization problem. 10
1. Multivariable optimization problem with no constraint.
 2. Multivariable optimization problem with equality constraint.
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