

[Time: Three Hours]

[Marks:80]

N.B.: (1) Question No 1 is compulsory**(2) Attempt any three questions out of the remaining five questions****(3) Non Programmable calculator is allowed****Q.1)**

- a) Find the value of the integral $\int_0^{1+i} (x - y + ix^2) dz$ along the straight line from $z=0$ to $z=1+i$. [5]
- b) Find the Fourier Series representing by $f(x) = |x|$, $-\pi < x < \pi$. [5]
- c) Find the Fourier transforms of $f(x) = 1$, $|x| < k$; 0 for $|x| > k$ [5]
- d) Express $f(x) = x^4 - 8x^3 + 18x^2 - 10x$. Find also the function whose first difference is the given function. [5]

Q.2)

- a) Expand $f(x) = lx - x^2$, $0 < x < l$ in a half range sine series [6]
- b) Using the method of Lagrange's multipliers solve the following NLPP Optimize $z = 6x_1 + 8x_2 - x_1^2 - x_2^2$ subject to $4x_1 + 3x_2 = 16$, $3x_1 + 5x_2 = 15$, $x_1, x_2 \geq 0$ [6]
- c) Expand $f(z) = \frac{2}{(z-1)(z-2)}$ about $z=0$ indicating the region of convergence. [8]

Q.3)

- a) If $f(5)=12$, $f(6)=13$, $f(9)=14$ and $f(11)=16$, find $f(10)$ using Lagrange's Interpolation formula [6]
- b) Find the solution of the wave equation $\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$ such that $y = P_0 \cos pt$, (P_0 is constant) when $x=L$ and $y=0$ when $x=0$ [6]
- c) Use the Kuhn Tucker conditions to solve the following NLPP [8]
Maximize $z = 10x_1 + 10x_2 - x_1^2 - x_2^2$
subject to $x_1 + x_2 \leq 8$,
 $-x_1 + x_2 \leq 5$, $x_1, x_2 \geq 0$

Q4)

- a) Find Half range cosine series for $f(x) = x$, $0 < x < 2$ [6]
- b) Evaluate the integral using Cauchy's Integral formula $\int_C \frac{e^{zz}}{(z-a)^4} dz$ where C is the circle $|z| = 2$ [6]
- c) A bar with insulated sides is initially at temperature $0^\circ C$ throughout. The end $x=0$ is kept at $0^\circ C$ and the heat is suddenly applied so that $\frac{\partial u}{\partial x} = 10$ at $x=L$ for all the time. Find the temperature function $u(x,t)$. [8]

Q5)

- a) Find $f(4.4)$ for which $f(0)=12, f(2)=7, f(4)=6, f(6)=7, f(8)=13, f(10)=32, f(12)=77$ [6]
 b) Find the complex form of the Fourier series for $f(x) = e^{2x}$ in $(0,2)$ [6]
 c) The steady state temperature distribution in a thin plate bounded by the lines $x=0, x=a, y=0$ and $y=\infty$ governed by the partial differential equation $U_{xx}+U_{yy}=0$. Obtain the steady state temperature distribution under the conditions:
 $U(0,y)=U(a,y)=U(x,\infty)=0$ and $U(x,0)=x, \quad 0 \leq x \leq \frac{a}{2},$ [8]
 $= a-x, \quad \frac{a}{2} \leq x \leq a.$

Q6)

- a) solve $\frac{\partial z}{\partial x} - 2 \frac{\partial z}{\partial y} = z$ where $z(x, 0) = 3e^{-5x} + 2e^{-3x}$ using method of separation of variable [6]
 b) Evaluate $\int_0^{2\pi} \frac{\cos 2\theta}{5+4\cos\theta} d\theta.$ [6]
 c) Use Newton's Divided Difference formula to find the polynomial of the lowest degree which assumes the following values: Also find $f'(2)$ and $f''(2)$ [8]

x	-1	1	2	3
f(x)	-21	15	12	3

 xxxxx
