

Signals & Control Systems

Q. P. Code : 50562

Time : 3 hours

Marks : 80

Question No. 1 is Compulsory.

Answer any three questions from the remaining five questions.

Assume any data if needed, clearly mention the assumption.

Use graph sheet for Q6 (a) and semi log graph for Q6(b)

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Q1)

- a) Find whether the following signal is periodic or not, if periodic find the period (4)
 $x(t) = 2 \cos^2(2\pi t)$
- b) Check whether the following system described by the impulse response $h(t) = 2e^{-t}u(t)$ is causal or not, stable or not, Justify (4)
- c) Find the Fourier transform of the signal $x(t) = e^{-2|t|}$, sketch the signal and its transform (4)
- d) Find the initial value and final value of the signal $X(s) = \frac{s+10}{s^2+2s+3}$ (4)
- e) Find the range of values of K, so that the system characteristic equation given by $s^4 + 5s^3 + 5s^2 + 4s + K = 0$ is stable (4)

Q2)

- a) Find the energy and power of the signal $x(t) = 2 \cos(3\frac{\pi}{4}t + \frac{\pi}{6})$ (6)
- b) Sketch the signal $x(t) = 1 - |t|$ for $|t| \leq 1$; $x(t) = 0$, elsewhere. (2)
Sketch also i) $x(1-2t)$ ii) $x(\frac{t}{3} - 1)$ (6)
- c) Find the output of the LTI system with impulse response $h(t) = u(t)$ and input $x(t) = e^{-2t}u(t)$, sketch the output (6)

Q3)

- a) Find whether the system given by input output relation is linear or not, time invariant or not, $y(t) = x(2t) + 3$; $x(t)$ is the input, $y(t)$ the output (6)
- b) Find out whether the following set of signals are orthogonal or not in the interval $0 \leq t \leq \frac{2\pi}{\omega_0}$, $x_k(t) = e^{jk\omega_0 t}$, $-\infty \leq k \leq +\infty$ (6)
- c) Calculate the trigonometric Fourier series co-efficients of a full wave rectifier output wave form when the input is a sine wave of frequency 50 Hz and amplitude is 'A' (8)

OC

Q4)

- a) Find the Frequency response and impulse response of the system described by the differential equation (6)

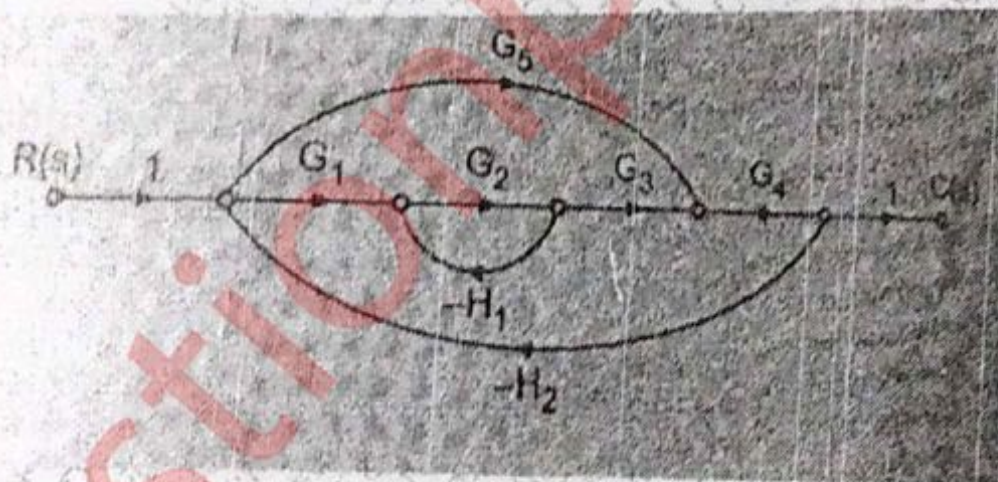
$$\frac{d^2y(t)}{dt^2} + 3 \frac{dy(t)}{dt} + 2y(t) = 2 \frac{dx(t)}{dt} + x(t)$$

- b) Find the inverse Laplace transform of $X(s) = \frac{-5s-7}{(s+1)(s-1)(s+2)}$ for all possible ROC (8)

- c) Find the Laplace transform of $x(t) = \frac{d^2(e^{-3(t-2)}u(t-2))}{dt^2}$; specify the ROC (6)

Q5)

- a) Explain Mason's gain formula and find $\frac{C(s)}{R(s)}$ using Mason's formula for the signal flow graph shown below (8)



- c) A unit step input is applied to the unity negative feedback system for which open loop Transfer function $G(s) = \frac{16}{s(s+8)}$ find i) its closed loop transfer function ii) Natural frequency of oscillation ω_n iii) Damping ratio ξ iv) damped frequency of oscillation ω_d (6)
- d) Explain the term Gain Margin and Phase margin (6)

Q6)

- a) Sketch the root locus for the system having $G(s)H(s) = \frac{k(s+5)}{s^2+4s+20}$ (10)
- b) A unity feed back control system is having $G(s) = \frac{80}{s(s+2)(s+20)}$ Draw the bode plot and comment on the stability of the feed back system (10)
