

Note: i) Q.No 1 is compulsory

ii) Attempt any three from remaining.

ii) All questions carry equal marks.

Q.No.1) a) If $\tanh x = \frac{1}{2}$, find $\sinh 2x$, $\cosh 2x$. (3)

b) If $z = xyf\left(\frac{y}{x}\right)$, prove that $x\frac{\partial z}{\partial x} + y\frac{\partial z}{\partial y} = 2z$ (3)

c) If $x = u(1-v)$, $y = uv - uvw$, $z = uvw$ find $\frac{\partial(x,y,z)}{\partial(u,v,w)}$ (3)

d) Using Maclaurin's expansion, Prove that (3)

$$e^x \sec x = 1 + x + \frac{2x^2}{2!} + \frac{4x^3}{3!} + \dots$$

e) Show that every square matrix A can be uniquely expressed as $P+iQ$, where P & Q are Hermitian Matrices. (4)

f) Find nth derivative of $e^x \cos x \cos 2x$ (4)

Q.No.2) a) If $x = \cos \theta + i \sin \theta$, $y = \cos \phi + i \sin \phi$, show that

$$\frac{x-y}{x+y} = i \tan \frac{\theta-\phi}{2} \quad (6)$$

b) For the following matrix A, find non singular matrices P and Q such that PAQ is

$$\text{in normal form and hence find the rank of A, } A = \begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 0 & -1 & -1 \end{bmatrix} \quad (6)$$

c) If $u = \operatorname{cosec}^{-1} \sqrt{\frac{x^{1/2} + y^{1/2}}{x^{1/3} + y^{1/3}}}$, show that (8)

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial xy} + y^2 \frac{\partial^2 u}{\partial y^2} = \frac{\tan u}{12} \left(\frac{13}{12} + \frac{\tan^2 u}{12} \right)$$

Q.No 3) a) For what values of λ , the system of equations $3x-y+4z=3$, $x+2y-3z=-2$, $6x+5y+\lambda z=-3$ has a unique solution. Determine the solution in each case. (6)

b) Find the maxima and minima of the function (6)

$$f(x,y) = x^3 + y^3 - 3x - 12y + 20$$

c) Show that $\tan^{-1} i \left(\frac{x-a}{x+a} \right) = \frac{i}{2} \log \left(\frac{x}{a} \right)$ (8)

Q.No.4) a) Find $\frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}$, using partial derivatives for (6)

$$xe^y + ye^z + \log x - 2 - 3 \log 2 = 0 \text{ at } P(1, \log 2, \log 3)$$

b) Find the principal value of $(1 + i)^{1-i}$. (6)

c) Solve the following system of equation by crouts method (8)

$$x + y + z = 3, \quad 2x - y + 3z = 16, \quad 3x + y - z = -3$$

Q.No.5) a) Show that $\frac{\sin 6\theta}{\sin 2\theta} = 16\cos^4\theta - 16\cos^2\theta + 3$ (6)

b) Find a and b such that $\lim_{x \rightarrow 0} \frac{x(1 - a\cos x) + b\sin x}{x^4} = \frac{1}{3}$ (6)

c) If $y = (1 - x)^{-\alpha} e^{-\alpha x}$, show that (8)

(i) $(1 - x)y_1 = \alpha xy$

(ii) $(1 - x)y_{n+1} - (n + \alpha)y_n - \alpha y_{n-1} = 0$

Q.No.6) a) Show that the rows of the following matrix are linearly dependent and find the

relationship between them $\begin{bmatrix} 1 & 0 & 2 & 1 \\ 3 & 1 & 2 & 1 \\ 4 & 6 & 2 & -4 \\ -6 & 0 & -3 & -4 \end{bmatrix}$ (6)

b) If $\phi\left(\frac{z}{x^3}, \frac{y}{x}\right) = 0$, prove that $px + qy = 3z$ (6)

c) Fit a second degree parabola to the following data (8)

x:	-2	-1	0	1	2
y:	-3.150	-1.390	.620	2.880	5.378

Course: F.E.(ALL BRANCHES) (CBSGS) (SEMESTER - I)(Prog T0121)

QP Code: 529302(2nd Query)

Correction:

Q. 6 c

Read As: **.620**

Query Update time: 07/12/2016 11:50 AM

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Course: F.E.(ALL BRANCHES) (CBSGS) (SEMESTER - I)(Prog T0121)

QP Code: 529302

Correction:

Q.1 B)

$$x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 2z \text{ read as } x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = 2z$$

Q.2 C)

$$x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial xy} + y^2 \frac{\partial^2 u}{\partial y^2} \text{ read this as } x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2}$$

Q.6 B) add the sentence

$$\text{Where } p = \frac{\partial z}{\partial x}, q = \frac{\partial z}{\partial y}$$

Query Update time: 07/12/2016 11:50 AM