

Instructions: -

3 Hours



Total Marks :80

- Question one is compulsory
- Assume suitable data if necessary

Q1. Attempt any four

- Define nonlinear system and write detail classification of nonlinearities of system
- Draw sinusoidal response of saturation with dead zone nonlinearity and write the response equation
- Explain Jump resonance for nonlinear system
- How to comment on stability using singular point.
- Explain in details about limit cycle.

Q2. (a) For following system find of stability using singular point and draw trajectories. (10)

$$1. \ddot{y} - 8\dot{y} + 17y = 34$$

$$2. \ddot{x} + \dot{x} + x^3 = 0$$

(b) Derive the describing function for relay with saturation. (10)

Q3. (a) Comment on Stability of the state space model given below using suitable Lyapunov function (10)

$$\dot{X}_1 = X_2 - X_1(X_1^2 + X_2^2)$$

$$\dot{X}_2 = -X_1 - X_2(X_1^2 + X_2^2)$$

(b) Investigate Stability using Describing function of following system which has unity relay signal as a nonlinearity. (10)



Q4. (a) Design IMC controller for plant model  $G(s) = \frac{-s+1}{(2s+1)}$  to achieve the response with time

constant of 1.5 Sec. (10)

(b) Design the optimal controller via Riccati equation for system

$$\dot{x} = \begin{bmatrix} 0 & 1 \\ 2 & -1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$$

To minimize the performance index  $J = \int_0^{\infty} (x_1^2 + x_2^2 + u^2) dt$  (10)

TURN OVER

Q5. (a) Determine stability using Krasovskii method

(10)

$$\dot{x}_1 = -x_1;$$

$$\dot{x}_2 = x_1 - x_2$$

(b) Using variable gradient method find suitable Lyapunov function for the system given by

(10)

$$\dot{x}_1 = x_2$$

$$\dot{x}_2 = -x_1^3 - x_2$$

Q6. (a) Explain in details IMC based PID controller Design/tuning.

(10)

(b) Draw Phase Trajectory using delta method for given system,

(10)

$$x^3 + 5x + 4x = 0$$

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