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O.P. Code:

(3 Hours)

[Total Marks: 100

N.B.: (1) Question Number 1 is compulsory.

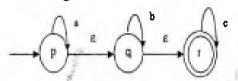
- (2) Attempt any three questions out of remaining five questions.
- (3) Assumptions made should be clearly stated.
- (4) Figures to the right indicate full marks.
- (5) Assume suitable data whenever required but justify the same.
- 1. (a) Consider the following grammar $G = (V, T, P, S), V = \{S, X\}, T \{0, 1\}$ and productions P are

 $S \rightarrow 0 \mid 0X1 \mid 01S1$

 $X \rightarrow 0XX1 \mid 1S$

S is start symbol. Show that above grammar is ambiguous. Q

- (b) State and prove the halting problem.
- (c) Convert following ε-NFA to NFA without ε.



- (d) Prove that Language $L = \{0^n \mid 0^n \text{ for } n = 0, 1, 2, \dots \}$ is not regular.
- 2. (a) Consider the following grammar $G \in (V, T, P, S)$, $V = \{S, X, Y\}$, $T \{a, b\}$ and productions P are

 $S \rightarrow XYX$

 $X \rightarrow aX \mid \epsilon$

 $Y \rightarrow bY | \epsilon$

Convert this grammar in Chomsky Normal Form (CNF).

- (b) Design DPDA to accept language L={ $x \in \{a, b\}^* | N_a(x) > N_b(x) \}$, 10 $N_a(x) > N_b(x)$ means number of a's are greater than number of b's in string x.
- 3. (a) Design Turing machine to accept the language L = set of strings with equal 10 number of a's and b's.
 - (b) Design the DFA to accept the language containing all the strings over 10 (a, b, c) that starts and ends with different symbols.

TURN OVER